

# HINTS & SOLUTIONS (PRACTICE PAPER-2)

## ANSWER KEY

Ques.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	D	A	A	A	C	C	B	D	D	B	C	B	C	B	A
Ques.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	A	D	A	D	C	D	C	A	D	B	C	A	C	D	B
Ques.	31	32	33	34	35	36	37	38	39	40					
Ans.	D	C	C	B	A	B	A	A	D	B					

PART - A (1 Mark)

## MATHEMATICS

1.  $\sqrt{x+5} \geq 0 \quad \therefore 1-x \geq 0$   
 $x < 1 \quad \dots(i)$   
 $\sqrt{x+5} > 1-x$   
 $x+5 > 1+x^2-2x$   
 $x^2-3x-4 < 0$   
 $(x-4)(x+1) < 0$   
 $x \in (-1, 4) \quad \dots(ii)$   
 Using (i) & (ii)  $x \in (-1, 1)$

3.  $x = x^2 + y^2$  &  $y = 2xy$   
 I when  $y = 0$   
 $\Rightarrow x = x^2$   
 $\Rightarrow x = 0, x = 1$   
 $\therefore$  solutions are (0,0) (1,0)

II when  $x = \frac{1}{2}$   
 $\Rightarrow \frac{1}{2} - \frac{1}{4} = y^2 \quad \Rightarrow \quad \frac{1}{4} = y^2 \quad \Rightarrow \quad y = \pm \frac{1}{2}$

$\therefore$  solutions  $\left(\frac{1}{2}, \frac{1}{2}\right) \left(\frac{1}{2}, -\frac{1}{2}\right)$

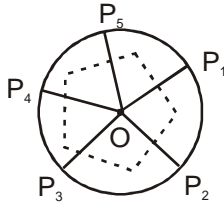
4.  $x^3 - 3|x| + 2 = 0 \quad [\text{Let } x > 0]$   
 $x^3 - 3x + 2 = 0$   
 $(x-1)(x^2+x-2) = 0$   
 $x = 1, x = \frac{-1+\sqrt{9}}{2} = 1$   
 Now, let  $x < 0$   
 $x^3 + 3x + 2 = 0$   
 no solution  
 $x = 1$  only one solution

5.  $(1+2x)^{20} = a_0 + a_1x + a_2x^2 + \dots + a_{20}x^{20}$   
 put  $x = 1$   $3^{20} = a_0 + a_1 + a_2 + \dots + a_{20}$   
 $x = -1$   $1 = a_0 - a_1 + a_2 - a_3 + \dots + a_{20}$   
 subtract  $3^{20} - 1 = 2(a_1 + a_3 + \dots + a_{19})$   
 add  $3^{20} + 1 = 2(a_0 + a_2 + \dots + a_{20})$

$$2(a_1 + a_3 + \dots + a_{19}) + 3[a_0 + a_2 + \dots + a_{20}] = (3^{20} - 1) + \frac{3}{2}(3^{20} + 1)$$

$$= \frac{5 \cdot 3^{20} + 1}{2}$$

6. Points which are equidistant from O and  $P_1$  lies on perpendicular bisector of  $OP_1$



Similarly for others

- $\therefore$  In figure points on pentagon are equidistant from points  $P_1, P_2, \dots$  and O  
 $\therefore$  interior region of pentagon is closed to 'O'

7. Let  $(x, y)$  be any point

Using given condition  $2\sqrt{(x-2)^2 + y^2} < 3\sqrt{(x-0)^2 + (y-3)^2}$

$$5x^2 + 5y^2 - 54y + 16x + 65 > 0$$

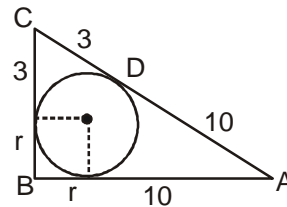
$$x^2 + y^2 - 10.8y + 3.2x + 13 > 0$$

It is a circle, radius =  $\sqrt{18.72}$

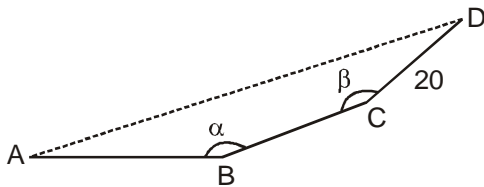
Centre  $(-1.6, 5.4)$

Hence region is exterior of  $(x + 1.6)^2 + (y - 5.4)^2 = 18.72$ .

8.  $(r + 3)^2 + (r + 10)^2 = (13)^2$   
 $\Rightarrow r^2 + 9 + 6r + r^2 + 100 + 20r = 169$   
 $\Rightarrow 2r^2 + 26r - 60 = 0$   
 $\Rightarrow r^2 + 13r - 30 = 0$   
 $\Rightarrow (r + 15)(r - 2) = 0$   
 $\Rightarrow r = 2$



9. To find possible interval value of 4th side minimum possible value of 4th side greater than 0 is 1.  
 For maximum possible value.



let angle  $\alpha, \beta$  are slightly smaller than  $180^\circ$

if  $\alpha, \beta = 180^\circ$

$AD = 35$

$\therefore$  maximum value of 4th side is 34

$\therefore 1, 2, 3, \dots, 34$  are possible value of 4th side

$\therefore 34$  values are possible.

$$10. \quad \frac{V'}{V} = \frac{172.8}{100} = \frac{\frac{4}{3}\pi R'^3}{\frac{4}{3}\pi R^3}$$

$$\frac{R'}{R} = 1.2$$

$$\text{Now, ratio of surface area} = \frac{S'}{S} = \frac{4\pi R'^2}{4\pi R^2} =$$

$$= \frac{S'}{S} = 1.44$$

Hence surface area increased by 44%

## PHYSICS

12. given mass of planet A =  $m_A$   
and mass of planet B =  $m_B$   
 $m_B = 8 m_A$

$$g_A = \frac{Gm_A}{r_A^2} \text{ and } g_B = \frac{Gm_B}{r_B^2}$$

$$\text{or } \frac{g_A}{g_B} = \frac{m_A}{m_B} \left( \frac{r_B}{r_A} \right)^2 \quad \dots\dots(i)$$

$$\therefore m_B = 8 m_A$$

$$\frac{4}{3}\pi r_B^3 d = 8 \left( \frac{4}{3}\pi r_A^3 d \right) \quad \Rightarrow \frac{r_B}{r_A} = 2$$

$$\frac{g_A}{g_B} = \frac{1}{8} \times 4 = \frac{1}{2}$$

20.  $g_B = 2g_A$   
 $A = \pi r^2$

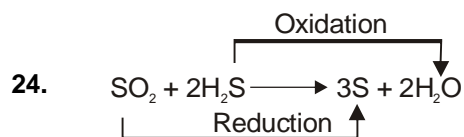
$$\frac{\Delta A}{A} = 2 \frac{\Delta r}{r}$$

$$\frac{\Delta A}{A} \% = 2 \left( \frac{\Delta r}{r} \right) \times 100$$

$$\frac{\Delta A}{A} \% = 2 \times 0.15 = 0.30\%$$

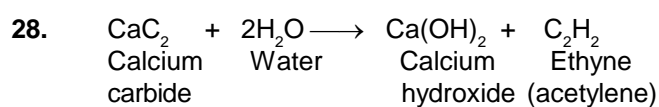
## CHEMISTRY


21. Silicon is tetravalent, so it forms  $\text{SiCl}_4$ .
22.  $\text{NH}_4\text{Cl}$  undergoes sublimation while  $\text{NaCl}$  does not.



26. As per Boyle's law  
 $PV = \text{constant}$

and  $P \propto \frac{1}{V}$



29. As we move downwards in a group, atomic radii increases. So the order will be  $\text{Li} < \text{Na} < \text{K} < \text{Cs}$ .
30.  $\text{CH}_3 - \text{C} \equiv \text{CH}$  (Propyne) and  (cyclo propene) are two possible structural isomers of  $\text{C}_3\text{H}_4$ .

DESCRIPTIVE TYPE ANSWER

PART - B (5 Mark)

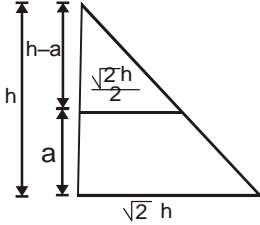
**MATHEMATICS**

1.

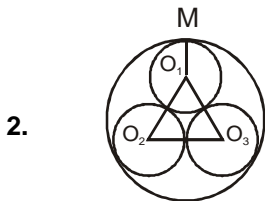
$$\frac{h-a}{h} = \frac{\frac{\sqrt{2}a}{2}}{\sqrt{2}h}$$

$$\frac{h-a}{1} = \frac{a}{2}$$

$$2h - 2a = a$$

$$2h = 3a$$


$$\frac{\text{volume of cone}}{\text{volume of cube}} = \frac{\frac{1}{3}\pi r^2 h}{a^3} = \frac{\frac{1}{3}\pi(\sqrt{2}h)^2 h}{\left(\frac{2h}{3}\right)^3} = 2.25$$



$O_1O_2 = O_2O_3 = O_3O_1 = 1 + 1 = 2$  unit  
 Height of equilateral triangle  $O_1O_2O_3$

$$= \frac{\sqrt{3}}{2} \times 2 = \sqrt{3} \text{ unit.}$$

Centre of the bigger circle O will be the centroid of the triangle.

$$O_1O = \frac{\sqrt{3} \times 2}{3} = \frac{2}{\sqrt{3}}$$

So, the radius of bigger circle

$$= \left(1 + \frac{2}{\sqrt{3}}\right) = \left(\frac{\sqrt{3} + 2}{\sqrt{3}}\right)$$

Hence, area of the bigger circle

$$= \pi \left(\frac{\sqrt{3} + 2}{\sqrt{3}}\right)^2$$

$$= \frac{\pi}{3} (2 + \sqrt{3})^2 \text{ sq. unit}$$

3.

$$(2^3)^{4^5} - (2^3)^{5^4}$$

Now as  $4^5 > 5^4$

{for  $x > 2, (x)^{x+1} > (x+1)^x$  always }

$$\therefore 2^{3^{4^5}} > 2^{3^{5^4}}$$

Now all even power of 3 are of the form  $4n + 1$

$\therefore$  last term of first digit is 2

also all odd powers of 3 are of the form  $4n + 3$ .

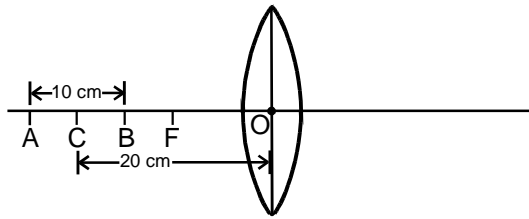
$\therefore$  last digit of the term is 8

[ $\therefore$  By cyclicity of last digit]

Thus, the last digit of expression  $2 - 8 = 4$ .

## PHYSICS

4.



In the given figure AB is the needle of length 10 cm.

CO = 20 cm, AO = 25 cm, BO = 15 cm

**For the image of end A of the needle:**

$u_1 = -25$  cm,  $f = 10$  cm.

$$\Rightarrow \frac{1}{v_1} - \frac{1}{u_1} = \frac{1}{f} \Rightarrow \frac{1}{v_1} = \frac{1}{10} + \frac{1}{-25} \Rightarrow \frac{1}{v_1} = \frac{1}{10} - \frac{1}{25} \Rightarrow \frac{1}{v_1} = \frac{3}{50}$$

$$\Rightarrow v_1 = 16.67 \text{ cm}$$

**For the image of end B of the needle:**

$u_2 = -15$  cm,  $f = 10$  cm.

$$\Rightarrow \frac{1}{v_2} - \frac{1}{u_2} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{v_2} - \frac{1}{-15} = \frac{1}{10} \Rightarrow \frac{1}{v_2} = \frac{1}{10} - \frac{1}{15}$$

$$\frac{1}{v_2} = \frac{1}{30} \Rightarrow v_2 = 30 \text{ cm}$$

Size of image of the needle AB =  $v_2 - v_1$

=  $30 - 16.67 = 13.33$  cm.

5. 
$$\frac{\text{Volume inside water}(u)}{\text{Total volume}(v)} = \frac{\text{Density of ice}}{\text{Density of sea water}}$$

$$\frac{u}{v} = \frac{0.92}{1.03}$$

$$\frac{u}{v} - 1 = \frac{0.92}{1.03} - 1$$

$$\frac{(u - v)}{v} = \frac{92 - 103}{103}$$

$$\text{or } \frac{(u - v)}{v} = \frac{11}{103}$$

$$\frac{\text{Volume out side water}}{\text{Total volume}} = \frac{11}{103} \times 100\% = \frac{1100}{103} \approx 11\%$$

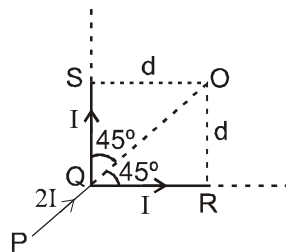
6. Magnetic field due to straight wire

PQ at O,

$$B_1 = 0$$

Magnetic field due to straight wire QR at O

$$B_2 = \frac{\mu_0 I}{4\pi d} (\sin \theta_1 + \sin \theta_2)$$



Here  $\theta_1 = 45^\circ$  and  $\theta_2 = 90^\circ$

$$B_2 = \frac{\mu_0 I}{4\pi d} \left( \frac{1}{\sqrt{2}} + 1 \right) \odot$$

Magnetic field due to wire QS at O

$$B_3 = \frac{\mu_0 I}{4\pi d} (\sin \theta_1 + \sin \theta_2)$$

Here  $\theta_1 = 45^\circ$  and  $\theta_2 = 90^\circ$

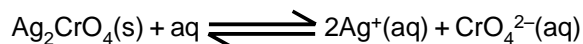
$$\text{So, } B_3 = \frac{\mu_0 I}{4\pi d} \left( \frac{1}{\sqrt{2}} + 1 \right) \otimes$$

Net magnetic field at O

$$B = B_1 + B_2 + B_3 = 0$$

## CHEMISTRY

7. Molarity of  $\text{Ag}_2\text{CrO}_4$  solution.



Let the solubility of  $\text{Ag}_2\text{CrO}_4$  in water be  $S$  mol litre<sup>-1</sup>. Then

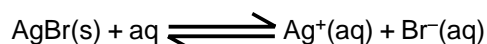
$$[\text{Ag}^+(\text{aq})] = 2S \text{ and } [\text{CrO}_4^{2-}(\text{aq})] = S$$

$$\text{Now, } K_{\text{sp}} = [\text{Ag}^+(\text{aq})]^2[\text{CrO}_4^{2-}(\text{aq})] = (2S)^2 \times S = 4S^3$$

$$\text{or } S = \sqrt[3]{\frac{K_{\text{sp}}}{4}} = \sqrt[3]{\frac{1.1 \times 10^{-12}}{4}} = 0.65 \times 10^{-4}$$

$$= 6.5 \times 10^{-5} \text{ mol L}^{-1}$$

(b) Molarity (or molar solubility) of Ag Br solution.



Let the solubility of AgBr be  $S$  mole L<sup>-1</sup>. Then  $[\text{Ag}^+(\text{aq})] = S$  and  $[\text{Br}^-(\text{aq})] = S$

$$\text{Now, } K_{\text{sp}} = [\text{Ag}^+(\text{aq})][\text{Br}^-(\text{aq})] = S \times S = S^2$$

$$\text{or } S = \sqrt{K_{\text{sp}}} = \sqrt{5.0 \times 10^{-13}}$$

$$= 0.707 \times 10^{-6} \text{ mol L}^{-1} = 7.07 \times 10^{-7} \text{ mol L}^{-1}$$

∴ Ratio of molarities of the saturated solutions

$$= \frac{\text{Molarity of } \text{Ag}_2\text{CrO}_4}{\text{Molarity of AgBr}} = \frac{6.5 \times 10^{-5}}{7.07 \times 10^{-7}} = 91.9$$

