

## PRACTICE PAPER

### CHEMISTRY

#### Q1.

Given that, for the reaction  $\text{H}^+(\text{aq}) + \text{OH}^-(\text{aq}) \rightarrow \text{H}_2\text{O}(\text{l})$ , energy released is 57.1 kJ. Three reactions are given as follows

- (1) 0.25 mole of HCl in solution is neutralized by 0.25 mole of NaOH; heat released is  $\Delta H_1$ .
- (2) 0.5 mole of  $\text{HNO}_3$  in solution is mixed with 0.2 mole of KOH solution; heat released is  $\Delta H_2$ .
- (3) 200  $\text{cm}^3$  of 0.2 M HCl solution is mixed with 300  $\text{cm}^3$  of 0.1 M NaOH solution heat released is  $\Delta H_3$ .

The correct order for the numerical value of  $\Delta H_1$ ,  $\Delta H_2$ ,  $\Delta H_3$  would be

- (a)  $\Delta H_1 > \Delta H_2 > \Delta H_3$
- (b)  $\Delta H_1 > \Delta H_3 > \Delta H_2$
- (c)  $\Delta H_3 > \Delta H_2 > \Delta H_1$
- (d)  $\Delta H_2 > \Delta H_1 > \Delta H_3$

#### Q2.

Given the following standard electrode potentials :

Element	Electrode reaction
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$E^\circ_{(298)}$	(Volts)
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$\text{Zn}/\text{Zn}^{2+}(\text{aq}) + 2\text{e}^- \rightarrow \text{Zn}(\text{s}) - 0.76$

$\text{Sn}/\text{Sn}^{2+}(\text{aq}) + 2\text{e}^- \rightarrow \text{Sn}(\text{s}) - 0.14$

$\text{Pb}/\text{Pb}^{2+}(\text{aq}) + 2\text{e}^- \rightarrow \text{Pb}(\text{s}) - 0.13$

$\text{Cu}/\text{Cu}^{2+} + 2\text{e}^- \rightarrow \text{Cu}(\text{s}) + 0.34$

Based on the above data, identify the correct answer. From an aqueous solution of the salts

- (a) Zinc can displace tin, lead, copper
- (b) Tin can displace zinc, lead, copper
- (c) Copper can displace zinc, tin, lead
- (d) Lead can displace zinc, tin, copper

**Q3.**

The electron energy for the quantum number  $n = 2$  in a hydrogen atom is

- (a)  $- 1.312 \times 10^6 \text{ Jmol}^{-1}$
- (b)  $- 3.28 \times 10^5 \text{ Jmol}^{-1}$
- (c)  $+ 3.28 \times 10^5 \text{ Jmol}^{-1}$
- (d)  $+ 1.312 \times 10^6 \text{ Jmol}^{-1}$

Given,  $m = 9.1 \times 10^{-31} \text{ kg}$ ;  $e = 1.6 \times 10^{-19} \text{ C}$ ;  $h = 6.6 \times 10^{-34} \text{ kgm}^2 \text{ s}^{-1}$

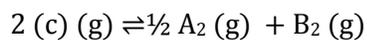
**Q4.**

The percent void space in close fcc packing of sphere is

- (a) 31.98 %
- (b) 25.96 %
- (c) 47.64 %
- (d) 74.04 %

**Q5.**

If the value for equilibrium constant for the reaction,  $A_2 (g) + 2 B_2 (g) \rightleftharpoons 4 C (g)$  is 2. What is the equilibrium constant for the reaction:



- (a) 2
- (b) 4
- (c)  $\sqrt{2}$
- (d)  $\frac{1}{\sqrt{2}}$

**Q6.**

Solution with reversed acidity and alkalinity are known as

- (a) Isotonic solutions
- (b) Iso-hydric solutions
- (c) Buffer solutions
- (d) None of these

**Q7.**

The rate of a second order reaction is  $5 \times 10^{-5} \text{ mol L}^{-1} \text{ S}^{-1}$ . When the initial concentration of the reactant is  $0.25 \text{ mol L}^{-1}$ , the value of the rate is

- (a)  $8 \times 10^{-4} \text{ Lmol}^{-1}$
- (b)  $2 \times 10^{-4} \text{ moll}^{-1}$
- (c)  $8 \times 10^{-4} \text{ molL}^{-1}$
- (d)  $2 \times 10^{-4} \text{ Lmol}^{-1}$

**Q8.**

The reverse of chemiluminescence is called

- (a) Fluorescence
- (b) Photochemical reaction
- (c) Phosphorescence
- (d) Photosensitization

**Q9.**

Which of the following molecules has unpaired electron in antibonding molecular orbital?

- (a)  $\text{O}_2$
- (b)  $\text{F}_2$
- (c)  $\text{N}_2$
- (d)  $\text{C}_2$

**Q10.**

The pH of a buffer solution containing 0.1M acetic acid and 0.1 M sodium acetate ( $\text{pK}_a$  of acetic acid is 4.74) is

- (a) 4.74
- (b) 5.74
- (c) 3.74
- (d) 9.48

**Q11.**

What is the hybridization of orbitals of boron and nitrogen, respectively, in  $\text{BF}_3 \cdot \text{NH}_3$ ?

- (a)  $\text{Sp}^2, \text{sp}^3$
- (b)  $\text{Dsp}^2, \text{sp}^3$
- (c)  $\text{Sp}^2, \text{sp}^2$
- (d)  $\text{Sp}^2\text{d}, \text{sp}^2$

**Q12.**

Which of the following compounds is used testing iron in its trivalent state to give intense blue colour for its confirmation?

- (a) KSCN
- (b)  $K_3 Fe (CM)_6$
- (c)  $K_4 Fe (CN)_6$
- (d)  $NH_4 NCS$

**Q13.**

The slag formed in blast furnace in metallurgy of iron is due to a reaction between:

- (a) Calcium &  $SiO_2$
- (b) Calcium carbonate &  $Fe_2O_3$
- (c) Calcium oxide &  $SiO_2$
- (d) Calcium chloride &  $Fe_2O_3$

**Q14.**

Which of the following compounds contains coordinate covalent bond?

- (a)  $N_2H_5^+$
- (b) HCl
- (c)  $BaCl_2$
- (d)  $H_2O$

**Q15.**

Which of the following compound does contain peroxide bridge?

- (a)  $Na_2O_2$
- (b)  $BaO_2$
- (c)  $H_2O_2$
- (d)  $SrO_2$

**Q16.**

Amongst the inert gases most abundant gas in the atmosphere is

- (a) He
- (b) Kr
- (c) Ne
- (d) Ar

**Q17.**

The Green House effect in the atmosphere is exhibited due to the presence of following as in atmosphere.

- (a)  $\text{CO}_2$
- (b)  $\text{O}_3$
- (c)  $\text{CO}$
- (d) all of these

**Q18.**

Which of the following has highest lattice energy?

- (a)  $\text{Be}(\text{OH})_2$
- (b)  $\text{Ca}(\text{OH})_2$
- (c)  $\text{Na}(\text{OH})_2$
- (d)  $\text{Ba}(\text{OH})_2$

**Q19.**

An atom or ion in an octahedral hole of a close packed structure has how many nearest neighbours?

- (a) 4
- (b) 8
- (c) 6
- (d) 12

**Q20.**

Out of the following values, which value is not correct for 20 volume solution of  $\text{H}_2\text{O}_2$ ?

- (a) It contains 60.7 gm/ltr of  $\text{H}_2\text{O}_2$
- (b) It is 6.07 % weight / volume
- (c) It is 1.8 molar solution of  $\text{H}_2\text{O}_2$
- (d) It liberates 40 litres of oxygen on decomposition.

**Q21.**

Besides  $\text{Ba}_2\text{O}$ ,  $\text{CaO}$  and  $\text{SiO}_2$ , pyrex glass contains two more oxides. Which of the following are correct?

- (a)  $\text{Fe}_2\text{O}_3$ ,  $\text{Al}_2\text{O}_3$
- (b)  $\text{PbO}$ ,  $\text{ZnO}$
- (c)  $\text{TiO}_2$ ,  $\text{B}_2\text{O}_3$
- (d)  $\text{B}_2\text{O}_3$ ,  $\text{Al}_2\text{O}_3$

**Q22.**

Which of the following reactions is not correct?

- (a)  $\text{SO}_3$  (in the presence of  $\text{H}_2\text{O}$ )  $\rightarrow$   $\text{H}_2\text{SO}_4$
- (b)  $\text{P}_2\text{O}_5$  (in the presence of  $\text{H}_2\text{O}$ )  $\rightarrow$   $\text{HPO}_3$
- (c)  $\text{N}_2\text{O}$  (in the presence of  $\text{H}_2\text{O}$ )  $\rightarrow$   $\text{HNO}_2$
- (d)  $\text{B}_2\text{O}_3$  (in the presence of  $\text{H}_2\text{O}$ )  $\rightarrow$   $\text{HBO}_2$

**Q23.**

Which of the following compounds is formed when 'hypo' dissolves silver bromide?

- (a)  $\text{Na}_3 [\text{Ag}(\text{S}_2\text{O}_3)_2]$
- (b)  $\text{Na}_2 [\text{Ag}(\text{SO}_3 \text{ Br})]$
- (c)  $\text{Na} [\text{Ag} (\text{SO}_3)_3]$
- (d)  $\text{Na} [\text{Ag} (\text{S}_2 \text{O}_3)_2]$

**Q24.**

Which of the following is the allotrope of carbon ?

- (a) Fullerene
- (b) Freon
- (c) Ferrocene
- (d) Furazine

**Q25.**

The diamagnetic species is

- (a)  $[\text{Ni} (\text{CN})_4]^{2-}$
- (b)  $[\text{NiCl}_4]^{2-}$
- (c)  $[\text{CoCl}_4]^{2-}$
- (d)  $[\text{CoF}_6]^{2-}$

**Q26.**

The product in the following reaction is:

- (a)  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_3$
- (b)  $(\text{CH}_3)_2\text{CH}_2\text{CH}_2\text{CH}_2\text{CH}_2\text{CH}_3$
- (c)  $(\text{CH}_3)_2\text{CH}_2\text{CH}_2\text{CH}_2\text{CH}_3$
- (d)  $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_3$

**Q27.**

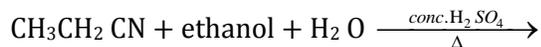
Nitration of aniline in strongly acidic medium, results in the formation of m- nitroaniline also

This is because

- (a) Amino group is meta orienting during electrophilic substitution reaction
- (b) Nitro group goes always to the meta position irrespective of the substituents
- (c) Nitration of aniline is a nucleophilic substitution reaction in strongly acidic medium
- (d) In strongly acidic conditions aniline is present as anilinium ion.

**Q28.**

State the product available by the following reaction.



- (a) Ethyl formate +  $\text{NH}_3$
- (b) Ethyl propanoate +  $\text{NH}_3$
- (c) Ethyl butanoate +  $\text{NH}_3$
- (d) Ethyl acetate +  $\text{NH}_3$

**Q29.**

An organic compound contains 49.3 % carbon 6.84 % hydrogen and its vapour density is 73. Molecular formula of the compound is

- (a)  $\text{C}_3\text{H}_8\text{O}_2$
- (b)  $\text{C}_3\text{H}_{10}\text{O}_2$
- (c)  $\text{C}_6\text{H}_{10}\text{O}_4$
- (d)  $\text{C}_4\text{H}_{10}\text{O}_2$

**Q30.**

Which is the most thermodynamically stable allotropic form of phosphorus?

- (a) Red
- (b) Black
- (c) White
- (d) Yellow

## PHYSICS

**Q1.**

A quantity  $X = \epsilon_0 L \frac{\Delta V}{\Delta t}$  where  $\epsilon_0$  is absolute permittivity,  $L$  is length,  $\Delta V$  is change in potential difference and  $\Delta t$  is change in time, Dimensions of  $X$  are same as that of

- (a) Resistance
- (b) Charge
- (c) Voltage
- (d) Current

**Q2.**

A player throws a ball upwards with an initial speed of  $294 \text{ ms}^{-1}$ . The height to which the ball rises and the time taken to reach the player's hands are assessed in different manners. The correct choice is

- (a) The height is 34.4 m
- (b) The time is 6s
- (c) The time is 3s
- (d) The height is 44 m

**Q3.**

A man fires a bullet of mass 200g at a speed of  $5\text{ms}^{-1}$  with a gun of 1kg mass. By what velocity the gun rebounds back?

- (a)  $0.1 \text{ ms}^{-1}$
- (b)  $10\text{ms}^{-1}$
- (c)  $1\text{ms}^{-1}$
- (d)  $0.01\text{ms}^{-1}$

**Q4.**

The moment of inertia of a square plate about a diagonal is  $I_d$  and that about a median is  $I_m$ , then

- (a)  $I_m = I_d$
- (b)  $I_m < I_d$
- (c)  $I_m > I_d$
- (d) None of these

Following question consists of two statements printed as Statement 1 and Statement 2. While answering these questions you are required to select any one of the response indicated as

1. if both statement 1 and Statement 2 are true and Statement 2 is a correct explanation of Statement 1.
2. If both Statement 1 and Statement 2 are true but the Statement 2 is not a correct explanation of Statement 1.
3. If Statement 1 is true but the Statement 2 is false.
4. If Statement 1 is false but Statement 2 is true.

**Q5.**

Statement 1 : Engine always works to keep a car moving  
Statement 2 : Engine always works to keep a car moving

- (a) 1
- (b) 2
- (c) 3
- (d) 4

**Q6.**

A quantity  $X = \epsilon_0 L \frac{\Delta V}{\Delta t}$  where  $\epsilon_0$  is absolute permittivity,  $L$  is length,  $\Delta V$  is change in potential difference and  $\Delta t$  is change in time. Dimensions of  $X$  are same as that of

- (a) Resistance
- (b) Charge
- (c) Voltage
- (d) Current

**Q7.**

A player throws a ball upwards with an initial speed of  $29.4 \text{ ms}^{-1}$ . The height to which the ball rises and the time taken to reach the player's hands are assessed in different manners. The correct choice is

- (a) The height is 34.4 m
- (b) The time is 6s
- (c) The time is 3s
- (d) The height is 44 m

**Q8.**

Three rods of equal length / are joined to form an equilateral triangle PQR. O is the mid point is PQ. Distance OR remains same for small change in temperature. Coefficient of linear expansion,  $\alpha_1$  for PR and  $\alpha_2$  for RQ are same. Then

- (a)  $\alpha_2 = 3 \alpha_1$
- (b)  $\alpha_2 = 4\alpha_1$
- (c)  $\alpha_1 = 3\alpha_2$
- (d)  $\alpha_1 = 4\alpha_2$

**Q9.**

If  $v$  is the mean speed,  $v_{\text{rms}}$  is the root mean square speed and  $V_p$  is the most probable speed of an ideal monoatomic gas at absolute temperature and mass of a gas molecule is  $m$ , then average kinetic energy of a molecule is

- (a)  $\frac{1}{2} mv^2$
- (b)  $\frac{3}{4} mv^2$
- (c)  $\frac{3}{4} mv_{\text{rms}}^2$
- (d)  $\frac{3}{4} mv_p^2$

**Q10.**

A simple pendulum with length  $l$  and bob mass  $m$  is executing SHM of small amplitude  $A$ . The maximum tension in the string will be

- (a)  $mg (1 + A/l)$
- (b)  $mg (1 + a/l)^2$
- (c)  $mg [1 + (A / l)^2]$
- (d)  $mg$

**Q11.**

The bob of a simple pendulum of length  $l$  is released at time  $t = 0$  from the position of small angular displacement  $\theta$ . Linear displacement of the bob at any time  $t$  is given as

- (a)  $l\theta \cos(gt/l)^{1/2}$
- (b)  $l\cos (gt / l)^{1/2}$
- (c)  $l\sin \theta$
- (d)  $l\theta \sin (gt/l)^{1/2}$

**Q12.**

1000 drops of water of radius 1 cm each carrying a charge of 10 esu combine to form a single drop. The capacitance of combined drop increases

- (a) 1 time
- (b) 10 times
- (c) 100 times
- (d) 1000 times

**Q13.**

The length of given cylindrical wire is increased by 100%. Due to consequent decrease in diameter the change in the resistance of the wire will be

- (a) 300 %
- (b) 200 %
- (c) 100 %
- (d) 50 %

Read the following paragraph

A thin magnetic needle has a time period of vibration as 6s in earth's magnetic field. It suddenly breaks into two pieces of half lengths. Let T be the time period of unbroken needle and T' be the time period of the broken piece.

Now answer the following questions:

**Q14.**

Ratio of moment of inertia of broken needle to normal is

- (a) 1 : 1
- (b) 1 : 2
- (c) 1 : 4
- (d) 1 : 8

**Q15.**

Ratio of magnetic moment of broken needle to normal needle is

- (a) 1 : 1
- (b) 1 : 2
- (c) 1 : 4
- (d) 1 : 8

**Q16.**

An inductor resistance battery circuit is switched on at  $t = 0$ . If the emf of battery is  $E$ , the charge passing through the battery in time constant  $T$  is

- (a)  $ET / Re$
- (b)  $eET / R$
- (c)  $ET / R\pi e$
- (d)  $2ET / eR$

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**Q17.**

Statement 1 : Energy currents of mechanical type have an aluminium disc.

Statement 2 : Eddy currents or Foucault's currents are produced in the metallic disc when it is rotated in the magnetic field to move the counters of the metre.

- (a) 1
- (b) 2
- (c) 3
- (d) 4

**Q18.**

An electromagnetic radiation has an energy 14.4 eV. To which region of electromagnetic spectrum does it belong?

- (a) Ultraviolet region
- (b) Visible region
- (c) X-ray region
- (d)  $\gamma$  - region

**Q19.**

To increase both the resolving power and magnifying power of a telescope

- (a) Both the focal length and aperture of the objective has to be increased.
- (b) The focal length of the objective has to be increased.
- (c) The aperture of the objective has to be increased.
- (d) The wavelength of light has to be decreased.

**Q20.**

H Polaroid is prepared by

- (a) Orienting herapathite crystals in the same direction
- (b) Using thin tourmaline crystals
- (c) Stretching polyvinyl alcohols and then heating with dehydrating agent
- (d) Stretching polyvinyl alcohol and then impregnating with iodine

**Q21.**

An ideal mirror has an area  $a$ . Light energy of frequency  $\nu$  and velocity  $c$  falling on this mirror per unit area is  $E$  for  $n$  photons in unit time. Then

- (a) No force is exerted on the mirror
- (b) A non calculable force exerts on the mirror
- (c) Force acted is given by  $2nh\nu/c$
- (d) No force but some pressure is exerted on the mirror.

**Q22.**

If the refractive index of a material of equilateral prism is  $\sqrt{3}$ , the angle of minimum deviation of the prism is

- (a)  $30^\circ$
- (b)  $45^\circ$
- (c)  $60^\circ$
- (d)  $75^\circ$

**Q23.**

A proton and an  $\alpha$  particle have kinetic energy in the ratio 16 : 1. The ratio of de Broglie waves associated with them is

- (a) 100 : 1
- (b) 200 : 1
- (c) 300 : 1
- (d) 400 : 1

**Q25.**

When a transistor is used in a circuit

- (a) The emitter base junction is forward biased and base collector junction is reverse biased
- (b) The emitter base junction is reverse biased and the base collector junction is forward biased
- (c) Both junctions are reverse biased.
- (d) None of these

**Q26.**

How many geo synchronous satellites are required to provide the communication over the whole part of the earth?

- (a) Minimum three
- (b) Minimum one
- (c) Minimum three
- (d) Minimum four

**Q27.**

An ionized gas contains both positive and negative ions. If it is subjected simultaneously to an electric field along the positive x direction and a magnetic field along the positive z direction, then

- (a) Positive ions deflect towards positive y direction and negative ion towards negative y direction
- (b) All ions deflect towards positive y direction
- (c) All ions deflect towards positive y direction
- (d) Positive ions deflect towards negative y direction and negative ions towards negative y direction

**Q28.**

A satellite is moving with a constant speed  $v$  in a circular orbit about the earth. An object of mass  $m$  is ejected from the satellite such that it just escapes from the gravitational pull of the earth. At the time of its ejection, the kinetic energy of the object is

- (a)  $\frac{1}{2}mv^2$
- (b)  $mv^2$
- (c)  $\frac{3}{2}mv^2$
- (d)  $2mv^2$

**Q29.**

An idea spring with spring constant  $k$  is hung from the ceiling and a block of mass  $M$  is attached to its lower end. The mass is released with the spring initially unstretched. The maximum extension in the spring is

- (a)  $\frac{4Mg}{k}$
- (b)  $\frac{2Mg}{k}$
- (c)  $\frac{Mg}{k}$
- (d)  $\frac{Mg}{k}$

**Q30.**

Two blocks of masses 10 kg and 4 kg are connected by a spring of negligible mass and placed on a frictionless horizontal surface. An impulse gives a velocity of 14 m/s to the heavier block in the direction of the lighter block. The velocity of the centre of mass is

- (a) 30 m/s
- (b) 20 m/s
- (c) 10 m/s
- (d) 5 m/s
- (e)

### MATHEMATICS

**Q1.**

In a survey of political preference, asked to give their preference on three government proposals I, II and III, 78% were in favor of at least on the proposals, 50% favored proposal I, 30% favored proposal II, 20% favored proposal III. If 5% favored all the three proposals, what % favored more than one of the three proposals?

- (a) 2
- (b) 11
- (c) 13
- (d) 17

**Q2.**

The range of the function  $f(x) = [\sin x]$  is

- (a)  $\{-1, 1\}$
- (b)  $[-1, 1]$
- (c)  $\{-1, 0, 1\}$
- (d)  $[0, 1]$

**Q3.**

The locus of a point  $z$  satisfying  $|2z - 1| = |z - 2|$  is a/an

- (a) Straight line
- (b) Circle
- (c) Ellipse
- (d) None of these

**Q4.**

The only root of  $ax^3 + bx + c = 0$ ,  $a \neq 0$ , is zero, if

- (a)  $c = 0$
- (b)  $c = 0, b \neq 0$
- (c)  $b = 0, c = 0$
- (d)  $b = 0, c \neq 0$

**Q5.**

If  $\alpha + \beta = 4$  and  $\alpha^3 + \beta^3 = 44$ ,  $\alpha, \beta$  are the roots of

- (a)  $2x^2 - 7x + 16 = 0$
- (b)  $3x^2 + 9x + 11 = 0$
- (c)  $9x^2 - 27x + 20 = 0$
- (d) None of these

**Q6.**

Let  $\Delta = \begin{vmatrix} a & a+b & a+b+c \\ 3a & 4a+3b & 5a+4b+3c \\ 6a & 9a+6b & 11a+9b+6c \end{vmatrix}$ , where

$a = i, b = w, c = w^2$ , then  $\Delta$  is equal to

- (a) -1
- (b) 1
- (c) -i
- (d) i

**Q7.**

The number of ways of painting the faces of a cube with six different colours is

- (a)  $2!$
- (b)  $3!$
- (c)  $6!$
- (d) None of these

**Q8.**

$${}^n C_0 - \frac{1}{2} {}^n C_1 + \frac{1}{3} {}^n C_2 + \dots + (-1)^n {}^n C_n / n + 1 =$$

- (a)  $n$
- (b)  $1/n$
- (c)  $\frac{1}{n+1}$
- (d)  $\frac{1}{n-1}$

**Q9.**

The sum of first two terms of an infinite G.P. is 1 and every term is twice the sum of the successive terms. Its first term is

- (a)  $\frac{1}{2}$
- (b)  $\frac{1}{3}$
- (c)  $\frac{2}{3}$
- (d)  $\frac{3}{4}$

**Q10.**

$$\frac{3+5+7+\dots+n \text{ terms}}{5+8+11+\dots+10 \text{ terms}} = 7, \text{ then the value of } n \text{ is}$$

- (a) 19
- (b) 22
- (c) 33
- (d) 35

**Q11.**

If the sum of an infinite G.P. is 3 and the sum of the square of its terms is also 3, then its first term and common ratio are

- (a)  $\frac{1}{2}, \frac{1}{3}$
- (b)  $\frac{3}{2}, \frac{1}{2}$
- (c)  $\frac{1}{3}, \frac{1}{4}$
- (d) None of these

**Q12.**

$$\text{Lt}_{x \rightarrow \infty} \left( \frac{x+5}{x+1} \right)^{x+4} \text{ is equal to}$$

- (a)  $e$
- (b)  $e^2$
- (c)  $e^3$
- (d)  $e^4$

**Q13.**

Lt  $x \rightarrow 0 \frac{1-\cos x}{x}$  is equal to

- (a) 0
- (b)  $\frac{1}{2}$
- (c) 1
- (d) does not exists

**Q14.**

Let  $f(x) = x^{3/2}$ , then  $f'(0) =$

- (a) 0
- (b)  $\frac{1}{2}$
- (c) 1
- (d) Does not exists

**Q15.**

If  $y = 4x - 5$  is tangent to the curve  $y^2 = px^3 + q$  at  $(2, 3)$ , then

- (a)  $p = 2, q = 3$
- (b)  $p = 2, q = -7$
- (c)  $p = 3, q = 7$
- (d)  $p = 2, q = -3$

**Q16.**

$$\int \sqrt{1 + \cos(x/4)} dx =$$

- (a)  $8\sqrt{2} \sin(x/8) + c$
- (b)  $-8\sqrt{2} \cos(x/8) + c$
- (c)  $8\sqrt{2} \sin\left(\frac{x}{4}\right) + c$
- (d) None of these

**Q17.**

$$\int \log x dx =$$

- (a)  $x(1 - \log x) + c$
- (b)  $x(\log x - 1) + c$
- (c)  $(1 + x) \log x + c$
- (d)  $(1 - x) \log x + c$

**Q18.**

$$\int_0^{\pi} \sqrt{1 - \cos x} \, dx =$$

- (a)  $\sqrt{2}$
- (b) 1
- (c) 2
- (d)  $2\sqrt{2}$

**Q19.**

The order of a differential equation whose solution is  $y = \alpha \cos x + b \sin x$ , where  $\alpha$  and  $b$  are arbitrary constants, is

- (a) 1
- (b) 2
- (c) 3
- (d) Cannot be determined

**Q20.**

If  $\frac{dy}{dx} + \frac{1}{y\sqrt{1-x^2}} = 0$ , then which of the following statements is true?

- (a)  $y^2 + 2\sin^{-1}x = c$
- (b)  $x^2 + 2\sin^{-1}y = c$
- (c)  $x^2 + 2\sin^{-1}x = c$
- (d) None of these

**Q21.**

The vertices of  $\Delta$  are  $(0, 0)$ ,  $(3, 0)$  and  $(0, 4)$ . Its orthocenter is at

- (a)  $(0, 0)$
- (b)  $(1/2, 1/2)$
- (c)  $(1/2, 3/2)$
- (d)  $(1, 3/2)$

**Q22.**

The equation  $\frac{x^2}{a^2} + \frac{x^2}{b^2} = 1$  represents a vertical ellipse if

- (a)  $a^2 = b^2$
- (b)  $a^2 > b^2$
- (c)  $a^2 < b^2$
- (d) None of these

**Q23.**

The points  $(5, -4, 2)$ ,  $(4, -3, 1)$ ,  $(7, -6, 4)$ ,  $(8, -7, 5)$  are the vertices of

- (a) Parallelogram
- (b) Square
- (c) Rectangle
- (d) Rhombus

**Q24.**

A particle acted on the constant forces  $4\hat{i} + \hat{j} - 3\hat{k}$  and  $3\hat{i} + \hat{j} - 3\hat{k}$  to the point  $5\hat{i} + 4\hat{j} + \hat{k}$ . the total work done by the forces is

- (a) 10 units
- (b) 20 units
- (c) 30 units
- (d) 0 units

**Q25.**

The probability that a man will live 10 more years is  $\frac{1}{4}$  and the probability that his wife will live 10 more years is  $\frac{1}{3}$ . then the probability that neither of them will be alive in 10 years is

- (a)  $\frac{11}{12}$
- (b)  $\frac{1}{2}$
- (c)  $\frac{7}{12}$
- (d) None of these

**Q26.**

Period of  $\cot 3x - \cos(4x + 3)$  is

- (a)  $\pi/3$
- (b)  $\pi/4$
- (c)  $\pi$
- (d)  $\pi/2$

**Q27.**

- (a)  $\sin^{-1}\frac{65}{56}$
- (b)  $\sin^{-1}\frac{56}{65}$
- (c)  $\cos^{-1}\frac{13}{25}$
- (d) None of these

**Q28.**

The area of the figure bounded by curves  $y^2 = 2x + 1$  and  $x - y = 1$  is

- (a)  $16/3$
- (b)  $18/3$
- (c)  $21/2$
- (d) None of these

**Q29.**

$\log(1 - x) = -\left(x + \frac{x^2}{2} + \frac{x^3}{3} + \dots\right)$  is valid for

- (a) all  $x \in \mathbb{R}$
- (b)  $-1 < x < 1$
- (c)  $-1 < x \leq 1$
- (d)  $-1 \leq x \leq 1$

**Q30.**

$1 + \log_e z + \frac{(\log_e z)^2}{2!} + \frac{(\log_e z)^3}{3!} + \dots$  is equal to

- (a)  $z$
- (b)  $z^{-1}$
- (c)  $\text{tog}z$
- (d) None of these