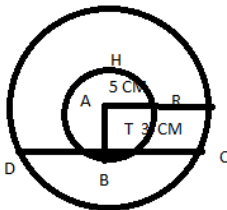


Class: X
Subject: Maths
Topic: Circles
No. of Questions: 20
Duration: 60 Min
Maximum Marks: 60

Question1: Two concentric circles are of radii 13 cm and 5 cm. The length of the chord of larger circle which touches the smaller circle is

- (a) 12 cm
- (b) 20 cm
- (c) 24 cm
- (d) 26 cm

Sol: (a)



A be Centre

$$R = 13 \text{ cm}$$

$$r = 5 \text{ cm}$$

$$AC = R \quad AB = r$$

$$BC = \sqrt{AC^2 - AB^2}$$

$$= \sqrt{13^2 - 5^2}$$

$$= 12$$

CD is the required chord which is

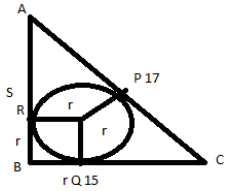
$$2BC = 24 \text{ cm (1r from center bisects the chord)}$$

Question2: A circle is inscribed in a triangle with sides 8, 15 and 17 cm. The radius of the circle is

- (a) 6 cm
- (b) 5 cm
- (c) 12 cm
- (d) 3 cm

Sol: (d) $8^2 + 15^2 = 17^2$

Hence it is a rt Δ



$AB = AR$
 $CP = CQ$
 $BQ = BR$

Tangents drawn from external point are equal in length

$$AP = AR = AB - r = 8 - r$$

$$PC = CQ = BC - r = 15 - r$$

$$AC = AP + PC = 23 - 2r = 17$$

$$R = 3 \text{ cm}$$

Question 3: From a point Q, the length of the tangent to a circle is 12 cm and the distance of Q from the centre is 13 cm. The radius of the circle is

- (a) 7 cm
- (b) 6.5 cm
- (c) 5 cm
- (d) 9 cm

Sol: (c) Radius $= \sqrt{13^2 - 12^2}$
 $= 5$

Question 4: If a line touches the circle at only one point, then it is known as

- (a) Chord
- (b) Secant
- (c) Tangent
- (d) Segment

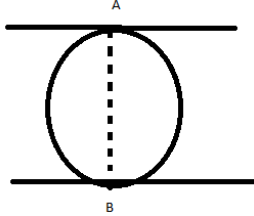
Sol: (c) Fact

Question 5: Two parallel lines touch the circle at points A and B respectively. The area of the circle is $25\pi \text{ cm}^2$, then AB is equal to

- (a) 5 cm
- (b) 8 cm
- (c) 10 cm

(d) 25 m

Sol: (c)



Clearly AB will be diameter
Area = $\pi r^2 = 25\pi$
 $r = 5$
Diameter = 10 cm

Question 6: A line is tangent to a circle with radius 5 cm. Distance between the centre of circle and the line m is

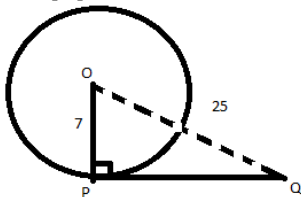
- (a) 3 cm
- (b) 4 cm
- (c) 5 cm
- (d) 6 cm

Sol: (c) Radius its distance

Question 7: A tangent PQ at a point P of a circle of radius 7 cm meets a line through centre O at a point Q so that OQ = 25 cm length PQ is

- (a) 20 cm
- (b) 14 cm
- (c) 24 cm
- (d) 26 cm

Sol: (c)



$$PQ = \sqrt{OQ^2 - OP^2}$$
$$= 24$$

Question 8: The common point of the tangent and the circle is called

- (a) Golden pint
- (b) Point of contact
- (c) Point of intersection
- (d) Degenerate point

Sol: (b) fact

Question 9: A line touches a circle of radius 4 cm. Another line is drawn which is tangent to the circle. If the two lines are parallel, then distance between them is

- (a) 4 cm
- (b) 6 cm
- (c) 7 cm
- (d) 8 cm

Sol: (d) distance between them is equal to its diameter

Question10: If a line intersects a circle in two distinct points, then it is known as a

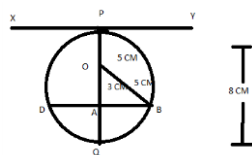
- (a) Chord
- (b) Secant
- (c) Tangent
- (d) Segment

Sol: (b) fact

Question11: At one end P of a diameter PQ of a circle of radius 5 cm, tangent XPY is drawn. The length of the chord RS parallel to XY and at a distance of 8 cm from P is :

- (a) 7 cm
- (b) 5 cm
- (c) 8 cm
- (d) 6 cm

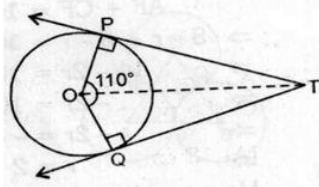
Sol: (c)



$$AB = \sqrt{5^2 + 3^2} = 4$$

$$B \Delta \text{ (required chord)} = 2 \times 4 = 8 \text{ cm}$$

Question12: In the given figure, If TP and TQ are two tangents to a circle with centre O, so that $\angle POQ = 110^\circ$, then $\angle PTQ$ is equal to :



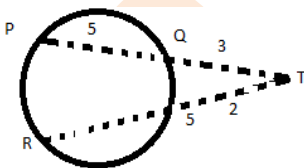
- (a) 60°
- (b) 90°
- (c) 70°
- (d) 80°

Sol: (c) $\angle PTQ = 360 - 110 - 90 - 90 = 70$

Question13: Two chords PQ and RS intersect at T outside the circle. If PQ = 5 cm, QT = 3 cm, TS = 2 cm. length of RS is :

- (a) 15 cm
- (b) 8 cm
- (c) 10 cm
- (d) 12 cm

Sol: (c)



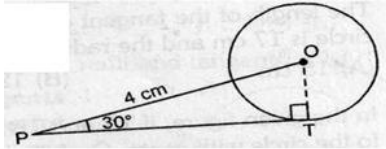
$$PT \times QT = RT \times ST$$

$$8 \times 3 = RT \times 2$$

$$: 12 = RT$$

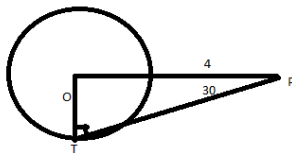
$$: RS = 12 - 2 = 10 \text{ cm}$$

Question14: In figure, PT is tangent to the circle with centre O such that OP is 4 cm and $\angle OPT=30^\circ$ length of tangent is given by :



- (a) $2\sqrt{3}$ cm
- (b) 5 cm
- (c) 7 cm
- (d) $4\sqrt{3}$ cm

Sol: (a)



$$\cos 30 = \frac{PT}{OP}$$

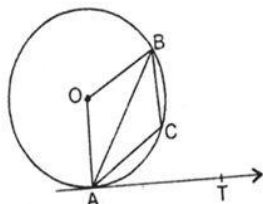
$$PT = OP \cos 30 = 4 \times \frac{\sqrt{3}}{2} = 2\sqrt{3} \text{ CM}$$

Question15: From a point Q, the length of tangent to a circle is 24 cm and the distance of Q from the centre is 25 cm, radius of circle is :

- (a) 8 cm
- (b) 7 cm
- (c) 6 cm
- (d) 10 cm

Sol: (b) Radius = $\sqrt{25^2 - 24^2}$
 = 7 cm

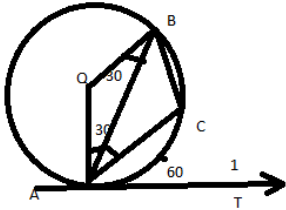
Question16: In figure, AB is a chord of a circle and AT is a tangent at A such that $\angle BAT=60^\circ$, measure of $\angle ACB$ is :



- (a) 120°
- (b) 90°

- (c) 150°
- (d) 110°

Sol: (a)



$$OAT = 90$$

(Radius and tangent are perpendicular)

$$\angle OAB + \angle BAT = 90$$

$$\angle OAB = \angle OBA = 30^\circ$$

$$\angle OAB = \angle OBA = 30 \text{ (Isosceles)}$$

$$\angle AOB = 120^\circ \text{ (}\angle \text{ sum Property)}$$

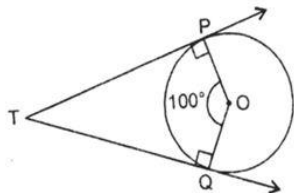
$$\text{Reflex } \angle AOB = 240^\circ$$

$$\angle BCA = \frac{1}{2} \text{ Reflex } \angle AOB$$

$$\angle BCA \text{ or } \angle ACB = 120^\circ$$

(\angle subtend by re at center is thrice the \angle subtended by it on the some segment)

Question17: In the adjacent figure, if TP and TQ are two tangents to a circle with centre O, so that $\angle PQQ=100^\circ$, then $\angle PTQ$ is equal to



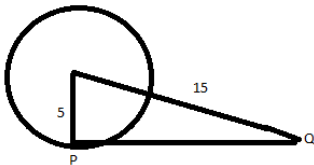
- (a) 80°
- (b) 60°
- (c) 40°
- (d) 90°

Sol: (a) $\angle PTQ = 360 - 100 - 90 - 90 = 80$

Question18: A tangent PQ at a point P of a circle of radius 5 cm meets a line through the centre O at a point Q, such that OQ = 15 cm. Length of PQ is

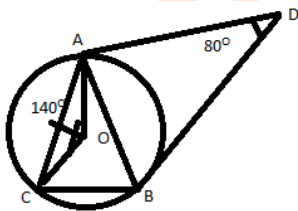
- (a) $10\sqrt{2}$ cm
- (b) 12 cm
- (c) $11\sqrt{9}$ cm
- (d) 13 cm

Sol: (a)



$$\begin{aligned} PQ &= \sqrt{15^2 + 5^2} \\ &= \sqrt{200} \\ &= 10\sqrt{2} \end{aligned}$$

Question19: In given figure, O is centre of the circumcircle of ΔABC . Tangents at A and B intersect at D. Given $\angle ADB = 80^\circ$ and $\angle AOC = 140^\circ$, calculate the $\angle ACB$.

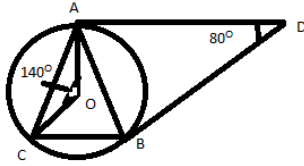


- (a) 20°
- (b) 40°
- (c) 60°
- (d) 80°

Sol: (c) AD and BD are tangents from an external point D to a circle with centre O.

$$\angle AD = BD$$

In ΔADB , we have $AD = BD$



$$\angle DAB = \angle DBC$$

[Since these are angles opposite to equal sides of a triangle]

$$180^\circ = \angle ADB + \angle DAB + \angle DBA$$

$$\Rightarrow 80^\circ + \angle DAB + \angle DBA = 180^\circ$$

$$\text{So, } \angle DAB + \angle DBA = 100^\circ$$

$$\Rightarrow \angle DAB = \angle DBA = 50^\circ$$

$OA \perp AD$ [\because The radius of a circle is perpendicular to the tangent through the point of contact]

$$\Rightarrow \angle OAD = 90^\circ$$

$$\angle OAB = \angle OAD - \angle DAB = 90^\circ - 50^\circ = 40^\circ$$

In $\triangle OAC$, we have

$$OA = OC \quad [\text{Radii of the same circle}]$$

$$\therefore \angle OAC = \angle OCA \quad [\angle\text{s opp. To equal sides}]$$

$$\text{But } \angle AOC = 140^\circ$$

$$\Rightarrow \angle OAC + \angle OCA = 180^\circ - \angle AOC = 180^\circ - 140^\circ = 40^\circ$$

$$\Rightarrow \angle OAC = \angle OCA = 20^\circ$$

$$\text{Now, } \angle CAB = \angle OAC + \angle OAB = 20^\circ + 40^\circ = 60^\circ.$$

Question20: In the diagram, O is the centre of the circle ABCD. The straight lines AC and BD intersect at O. The tangent at A meets CD Produced at E and $\angle AED = 32^\circ$. Calculate $\angle ABD$ and $\angle AOB$

(a) $58^\circ, 116^\circ$

(b) $62^\circ, 124^\circ$

(c) $44^\circ, 88^\circ$

(d) $58^\circ, 124^\circ$

Sol: (a) Since A, B, C, D are four points on circle having centre O and AC and BD intersect at O.

So, $OA = OB = OC = OD$. Since EA is tangent at A, $OA \perp EA$.

In ΔAOB , $OA = OB \Rightarrow \angle BAO = \angle ABO$. So, it is isosceles.

Similarly, ΔDOC is also isosceles

$$\angle ABD = \angle CAB = \angle BDC = \angle ACD.$$

From right angle ΔEAC

$$\angle ACE = 90^\circ - 32^\circ = 58^\circ$$

$$\angle ACE \text{ is } \angle ACD = \angle ABD.$$

$$\text{So, } \angle ABD = 58^\circ$$

$$(B) \angle AOB = \angle DOC \text{ and } \angle AOB + \angle OAB + \angle OBA = 180^\circ$$

$$\Rightarrow \angle AOB + 2 \times 58 = 180 \Rightarrow \angle AOB = 180 - 116$$

$$\Rightarrow \angle AOB = 64^\circ = \angle DOC$$

$$\angle AOD = 180 - \angle DOC = 180 - 64$$

$$\text{So, } \angle AOD = 116^\circ$$