

Class: X
Subject: Maths
Topic: Quadratic Equations
No. of Questions: 20
Duration: 60 Min
Maximum Marks: 60

Q1. The equation $x - \frac{7}{x-3} = 3 - \frac{7}{x-3}$ has _____.

- A. One integral root
- B. No root
- C. Two real roots
- D. Infinitely many roots

Solutions: B

Common mistake student cancels $7/x-3$ from both side and write $x=3$
But x cannot be 3 as at that value $7/x-3$ will not be defined. So no root.

Q2. The positive value of k for which the equation $x^2 + kx + 64 = 0$ and $x^2 - 8x + k = 0$ will both have real roots, is _____.

- A. None of these
- B. 8
- C. 12
- D. 16

Solutions: D

Apply $D \geq 0$ for both equations and find values which satisfies both conditions.

Q3. If the quadratic equation $kx(x - 2) + 6 = 0$ has equal roots, then the value of 'k' is

- A. 5
- B. 6
- C. 4
- D. 3

Solutions: B

$$D = 4k^2 - 24k = 0$$
$$k = 6$$

Q4. The root/roots of $\sqrt{2x - 3} + \sqrt{3x - 5} - \sqrt{5x - 6} = 0$ is/are _____.

- A. 2
- B. $7/6$
- C. 2 or $7/6$
- D. $\pm 1/3$

Solutions: A

Best method is to substitute and check which of them satisfies Otherwise take one term on RHS and square both sides. Simplify and get rational terms on 1 side and irrational on other. Again square both sides. and solve for x .

Q5. If $x = 1$ is a common root of the equations $ax^2 + ax + 3 = 0$ and $x^2 + x + b = 0$, then ab is equal to _____.

- A. 3
- B. 3.5
- C. 6
- D. -3

Solutions: A

Put 1 in both equations
from 1st equation $a = -3/2$
from 2nd equation $b = -2$
 $ab = 3$

Q6. The graph of the equation $y = ax^2 + bx + c$ has shape open upwards like 'U' which is known as parabola, when _____.

- A. $a < 0$
- B. $a > 0$
- C. $a = 0$
- D. $a \neq 0$

Solutions: B

Coefficient of $x^2 > 0$ for upward parabola

Q7. The roots of $(x^2 - 3x + 2)(x)(x - 4) = 0$ are _____.

- A. 4
- B. 0 and 4
- C. 0, 1, 2 and 4
- D. 1, 2 and 4

Solutions: C

Factorize first polynomial as $(x-2)(x-1)$
So roots will be 2,1,0,4

Q8. The equation $\sqrt{x+4} - \sqrt{x-3} + 1 = 0$ has _____.

- A. No real root
- B. One real root
- C. One real and one imaginary root
- D. Two imaginary roots

Solutions: A

Either do it by hit and trial if you are good in calculations otherwise or follow the squaring method.

By observation in this case $\text{root}(x+4) > \text{root}(x-3)$

So $\text{root}(x+4) + 1 > \text{root}(x-3)$

$\text{root}(x+4) - \text{root}(x-3) + 1 > 0$

So no real solution

- Q9.** If the equation $(a^2 + b^2)x^2 - 2(ac + bd)x + c^2 + d^2 = 0$ has equal roots, then _____.
- A. $ab = cd$
 - B. $ad = bc$
 - C. $ad = \frac{2c}{\sqrt{bc}}$
 - D. $ab = cd$

Solutions: B

Find discriminant and put it=0

- Q10.** The roots of $ax^2 + bx + c = 0$, $a \neq 0$ are real and unequal, if $b^2 - 4ac$ is _____.
- A. $= 0$
 - B. > 0
 - C. < 0
 - D. ≥ 0

Solutions: B

Fact

- Q11.** A man walks a distance of 48 km in a given time. If he walks 2 km/hr faster, he will perform the journey 4 hrs before. His normal rate of walking, is _____.
- A. 3 km/hr
 - B. 4 km/hr
 - C. - 6 km/hr or 4 km/hr
 - D. 5 km/hr

Solutions: B

Let x be speed and y be time taken

$$xy = 48$$

$$(x+2)(y-4) = 48 = xy$$

$$xy + 2y - 4x - 8 = xy$$

$$2y - 4x - 8 = 0$$

$$\text{Again } x = 48/y$$

Substitute and solve the quadratic equation.

- Q12.** A convex polygon has 44 diagonals. The number of its sides is _____.
- A. 10
 - B. 11
 - C. 12
 - D. 13

Solutions: B

Let n be number of sides of polygon.

$$(n-3) + (n-4) + (n-5) + \dots + n - (n-1) = 44$$

$$n(n-3) - (3+4+5+6+ \dots + n-1) = 44 \text{ (there } n-3 \text{ terms)}$$

Simplify both to get n

Q13. If $\frac{b}{x-a} = \frac{x+a}{b}$, then the value of x in terms of a and b is _____.

- A. $\pm\sqrt{a^2 + b^2}$
- B. $3 + \sqrt{a^2 + b^2}$
- C. $3 - \sqrt{a^2 + b^2}$
- D. $\pm\sqrt{a^2 - b^2}$

Solutions: A

$$b^2 = (x+a)(x-a)$$

$$b^2 = x^2 - a^2$$

$$x^2 = a^2 + b^2$$

Q14. The discriminant of the quadratic equation $3\sqrt{3}x^2 + 10x + \sqrt{3} = 0$ is

- A. 64
- B. 60
- C. 62
- D. 72

Solutions: A

$$D = 10^2 - 4(3\sqrt{3}\sqrt{3}) = 100 - 36 = 64$$

Q15. The nature of the roots of the equation $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$ is

- A. none of these
- B. not real
- C. real and equal
- D. real and unequal

Solutions: D

$$D = (-2\sqrt{2})^2 - 4(\sqrt{3})(-2\sqrt{3}) = 8 + 24 = 32 > 0$$

Q16. If one root of the equation $a(b-c)x^2 + b(c-a)x + c(a-b) = 0$ is 1, then the other root is _____.

- A. $b(c-a) / a(b-c)$
- B. $c(a-b) / a(b-c)$
- C. $b(c-a) / a(b-c)$
- D. $a(b-c) / c(a-b)$

Solutions: D

Use the relation between coefficients and roots

Product of roots = constant term / coefficient of x^2

Q17. In the equation $\frac{x(x-1) - (m+1)}{(x-1)(m-1)} = \frac{x}{m}$, the roots are equal when _____.

- A. $m = \frac{1}{2}$
- B. $m = -\frac{1}{2}$
- C. $m = 0$
- D. $m = 1$

Solutions: B

Cross Multiply and Simply and get D and equate it to 0

Q18. If $\sqrt{x-1} - \sqrt{x+1} + 1 = 0$, then $4x$ is equal to _____.

- A. $4\sqrt{-1}$
- B. $\frac{5}{4}$
- C. 5
- D. $1\frac{1}{4}$

Solutions: C

Take root(x+1) on other side and square both sides and simply to get $x = \frac{5}{4}$.

The roots of $ax^2 + bx + c = 0$, $a \neq 0$ are real, if $b^2 - 4ac$ is _____.

Q19.

- A. = 0
- B. ≥ 0
- C. ≤ 0
- D. > 0

Solutions: B

Fact

Q20. The value of k , if the expression $x^2 + kx + 1$ is factorisable into two linear factors, is _____.

- A. $k \leq 2$
- B. $k \geq -2$
- C. Either $k \geq 2$ or $k \leq -2$
- D. $-2 \leq k \leq 2$

Solutions: C

Two linear factor means roots are real and distant

$$k^2 - 4 > 0$$

$$k^2 > 4$$

$$k > 2 \text{ or } k < -2$$