

**Class: 11**  
**Subject: Math's**  
**Topic: Quadratic Equations**  
**No. of Questions: 25**

- The number of solutions of  $\sqrt{4-x} + \sqrt{x+9} = 5$  is
  - 0
  - 1
  - 2
  - 3
- The value of a for which one root of the quadratic equation,  $(a^2 - 5a + 3)x^2 + (3a - 1)x + 2 = 0$  is twice as large as other, is
  - 2/3
  - 1/3
  - 1/3
  - 2/3
- If  $f(x) = x^2 + 2bx + 2c^2$  and  $g(x) = -x^2 - 2cx + b^2$  are such that  $\min f(x) > \max g(x)$ , then the relation between b and c, is
  - no relation
  - $0 < c < b/2$
  - $|c| < \frac{|b|}{\sqrt{2}}$
  - $|c| > \sqrt{2}|b|$

4. Let  $p$  and  $q$  be the roots of  $x^2 - 2x + A = 0$  and let  $r$  and  $s$  be the roots of  $x^2 - 18x + B = 0$ . If  $p < q < r < s$  are in an A.P. then the ordered pair  $(A, B)$  is equal to
- A.  $(-3, 77)$   
B.  $(77, -3)$   
C.  $(-3, -77)$   
D. None of these
5. Suppose  $a, b, c$  are three non-zero real numbers. The equation  $x^2 + (a + b + c)x + (a^2 + b^2 + c^2) = 0$  has
- A. two negative real roots  
B. two positive real roots  
C. two real roots with opposite signs  
D. no real roots
6. The equation  $(\cos p - 1)x^2 + (\cos p)x + \sin p = 0$  in variable  $x$  has real roots, if  $p$  belongs to the interval
- A.  $(0, 2\pi)$   
B.  $(-\pi, 0)$   
C.  $(-\pi/2, \pi/2)$   
D.  $(0, \pi)$
7. If  $a, b$  are two real numbers satisfying the relations  $2a^2 - 3a - 1 = 0$  and  $b^2 + 3b - 2 = 0$  and  $ab \neq 1$ , then the value of  $\frac{ab + a + 1}{b}$  is
- A. 1  
B. 0  
C. 1  
D. 2

8. Suppose  $a, b, c$  are the lengths of three sides of a  $\triangle ABC$ ,  $a > b > c$ ,  $2b = a + c$  and  $b$  is a positive integer. If  $a^2 + b^2 + c^2 = 84$ , then the value of  $b$  is
- A. 7  
B. 6  
C. 5  
D. 4
9. Let  $p$  and  $q$  be real numbers such that  $p \neq 0$ ,  $p^3 \neq q$  and  $p^3 \neq -q$ . If  $\alpha$  and  $\beta$  are non-zero complex numbers satisfying  $\alpha + \beta = -p$  and  $\alpha^3 + \beta^3 = q$ , then a quadratic equation having  $\frac{\alpha}{\beta}$  and  $\frac{\beta}{\alpha}$  as its roots is
- A.  $(p^3 + q)x^2 - (p^3 + 2q)x + (p^3 + q) = 0$   
B.  $(p^3 + q)x^2 - (p^3 - 2q)x + (p^3 + q) = 0$   
C.  $(p^3 - q)x^2 - (5p^3 - 2q)x + (p^3 - q) = 0$   
D.  $(p^3 - q)x^2 - (5p^3 + 2q)x + (p^3 - q) = 0$
10. If  $a$  is the minimum root of the equation  $x^2 - 3|x| - 2 = 0$ , then the value of  $-1/a$  is
- A.  $(\sqrt{17} - 3)/4$   
B.  $(\sqrt{17} + 3)/4$   
C. 2  
D. 3
11. Let  $\alpha, \beta$  be the roots of  $x^2 - x + p = 0$  and  $\gamma, \delta$  be the roots of  $x^2 - 4x + q = 0$ . If  $\alpha, \beta, \gamma, \delta$  are in a G.P. then the integral values of  $p$  and  $q$  respectively, are
- A. 2, -32  
B. 2, 3  
C. 6, 3  
D. 6, -32

12. If  $\alpha$  and  $\beta$  ( $\alpha < \beta$ ) are the roots of the equation  $x^2 + bx + c = 0$ , where  $c < 0 < b$ , then
- A.  $0 < \alpha < \beta$
  - B.  $\alpha < 0 < \beta < |\alpha|$
  - C.  $\alpha < \beta < 0$
  - D.  $\alpha < 0 < |\alpha| < \beta$
13. If the roots of the equation  $x^2 - 2ax + a^2 + a - 3 = 0$  are real and less than 3, then
- A.  $a < 2$
  - B.  $2 \leq a \leq 3$
  - C.  $3 < a \leq 4$
  - D.  $a > 4$
14. If  $4^x - 3^{x-1/2} = 3^{x+1/2} - 2^{2x-1}$ , then the value of  $x$  is equal to
- A.  $5/2$
  - B.  $2$
  - C.  $3/2$
  - D.  $1$
15. The number of solutions of  $\sqrt{x+1} - \sqrt{x-1} = 1$ , ( $x \in \mathbb{R}$ ) is
- A. 1
  - B. 2
  - C. 4
  - D. Infinite
16. The equation  $\sqrt{x+1} - \sqrt{x-1} = \sqrt{4x-1}$ , ( $x \in \mathbb{R}$ ) has
- A. no solution
  - B. one solution
  - C. two solutions
  - D. more than two solutions

17. If  $c, d$  are roots of  $x^2 - 10ax - 11b = 0$  and  $a, b$  are roots of  $x^2 - 10cx - 11d = 0$ , then the value of  $a + b + c + d$  is
- A. 1210  
B. 1  
C. 2530  
D. 11
18. If the sum of the roots of the quadratic equation  $ax^2 + bx + c = 0$ , is equal to the sum of the squares of their reciprocals, then
- A.  $ab^2, ca^2, bc^2$  are in A.P.  
B.  $ab^2, bc^2, ca^2$  are in A.P.  
C.  $ab^2, bc^2, ca^2$  are in G.P.  
D. none of these
19. If  $a$  and  $b$  are the non-zero distinct roots of  $x^2 + ax + b = 0$ , then the least value of  $x^2 + ax + b$  is
- A.  $\frac{2}{3}$   
B.  $\frac{9}{4}$   
C.  $\frac{9}{4}$   
D. 1
20. If  $a < b < c < d$ , then the equation  $3(x - a)(x - c) + 5(x - b)(x - d) = 0$  has
- A. real and distinct roots  
B. real and equal roots  
C. purely imaginary roots  
D. none of these
21. Convert in the polar form  $\frac{1+7i}{(2-i)^2}$

22. Find the real values of  $x$  and  $y$  if  $(x - iy)(3 + 5i)$  is the conjugate of  $-6 - 24i$

23. If  $|z_1| = |z_2| = 1$ , prove that  $\left| \frac{1}{z_1} + \frac{1}{z_2} \right| = |z_1 + z_2|$

24. If  $\alpha$  and  $\beta$  are different complex number with  $|\beta| = 1$  then find  $\left| \frac{\beta - \alpha}{1 - \alpha\beta} \right|$

25. If  $\alpha + ib = \frac{(x+i)^2}{2x-i}$  prove that  $a^2 + b^2 = \frac{(x^2+1)^2}{4x^2+1}$