

Class: XI
Subject: Physics
Topic: Gravitation
No. of Questions: 20

Q1. The acceleration due to gravity g on earth is 9.8 ms^{-2} . What would be the value of g for a planet whose size is the same as that of the earth but the density is twice that of the earth?

- a. 19.6 ms^{-2}
- b. 9.8 ms^{-2}
- c. 4.9 ms^{-2}
- d. 2.45 ms^{-2}

Sol: a

Volume of earth (V) = $\frac{4\pi}{3} R^3$. Therefore, density of earth is $\rho = \frac{M}{V}$ or $M = V\rho = \frac{4\pi}{3} R^3 \rho$

Now $g = \frac{GM}{R^2} = \frac{4\pi G\rho R}{3}$. Since R is the same for both planets, if ρ is doubled, the value of g is also doubled. Hence the correct choice is (1).

Q2. If the radius of the earth suddenly decreases to 80% of its present value (the mass of the earth remaining the same), then the value of acceleration due to gravity will

- a. remain unchanged
- b. become $(9.8 \times 0.8) \text{ ms}^{-2}$
- c. increase by 36%
- d. increase by about 56%

Sol: d

Now $g = \frac{GM}{R^2}$. If R reduces to $R' = 0.8 R$, the value of g becomes

$$g' = \frac{GM}{R'^2} = \frac{GM}{0.64R^2}$$
$$= \frac{g}{0.64} = \frac{9.8 \text{ ms}^{-2}}{0.64}$$

$$\text{Increase in value of } g = \frac{g}{0.64} - g = \frac{0.36g}{0.64}$$

$$\therefore \text{Percentage increase} = \frac{0.36g}{0.64g} \times 100 = 56.25\%$$

Hence the correct choice is (4).

Q3. A small planet is revolving around a massive star in a circular orbit of radius R with a period of revolution T . If the gravitational force between the planet and the star is proportional to $R^{-5/2}$, then T will be proportional to

- a. $R^{3/2}$
- b. $R^{3/5}$
- c. $R^{7/2}$
- d. $R^{7/4}$

Sol: d

Since the gravitational force provides the necessary centripetal force for circular motion, we have

$$\frac{mv^2}{R} \propto R^{-5/2}$$

or $\frac{mv^2}{R} = kR^{-5/2}$, where k is a constant.

$$\text{Therefore } v = \sqrt{\frac{kR^{-3/2}}{m}}$$

Period of revolution $T = \frac{2\pi R}{v} = 2\pi \sqrt{\frac{m}{k}} \times R^{7/2}$ or
 $T \propto R^{7/4}$. Hence the correct choice is (4).

Q4. A satellite is orbiting the earth in a circular orbit of radius r . Its period of revolution varies as

- a. \sqrt{r}
- b. r
- c. $r^{3/2}$
- d. r^2

Sol: c

The speed of the satellite is given by

$$v = \sqrt{\frac{GM}{r}}$$

Therefore, its period of revolution is

$$T = \frac{2\pi r}{v} = \frac{2\pi}{\sqrt{GM}} \cdot r^{3/2}$$

Hence the correct choice is (3).

Q5. The angular momentum of the earth revolving around the sun is proportional to R^n , where R is the distance between the earth and the sun. The value of n is

- a. 0.5
- b. 1.0
- c. 1.5
- d. 2.0

Sol: a

We know that

$$\frac{mv^2}{R} = \frac{GMm}{R^2}$$

which gives $v = \sqrt{\frac{GM}{R}}$

Now, angular momentum $L = mvR = m \times \sqrt{\frac{GM}{R}} \times R$
 $= m\sqrt{GM} R^{1/2}$.
or $L \propto R^{1/2}$. Hence the correct choice is (1).

Q6. A satellite orbiting the earth is kept moving by the centripetal force provided by

- a. the burning of fuel in its engine
- b. the ejection of hot gases from its exhaust
- c. the gravitational attraction of the sun
- d. the gravitational attraction of the earth

Sol: d

Q7. Two satellites A and B are orbiting around the earth in circular orbits of the same radius. The mass of A is 16 times that of B. The ratio of the period of revolution of B to that of A is

- a. 1 : 16
- b. 1 : 4
- c. 1 : 2
- d. 1 : 1

Sol: d

The period of revolution of a satellite in a given orbit is independent of its mass. Hence, the correct choice is (4).

Q8. A satellite is moving around the earth in a stable circular orbit. Which one of the following statements will be wrong for such a satellite?

- a. It is moving at a constant speed.
- b. Its angular momentum remains constant.
- c. It is acted upon by a force directed away from the centre of the earth which counter-balances the gravitational pull of the earth.
- d. It behaves as if it were a freely falling body.

Sol: c

Choices (1), (2) and (4) are correct. Hence, choice (3) is the correct answer.

Q9. The escape velocity from Earth is v_e . What is the escape velocity from a planet whose radius is twice that of the Earth and mean density is the same as that of Earth?

- a. $v_e/2$
- b. v_e
- c. $2v_e$
- d. $4v_e$

Sol: c

For earth : $v_e = \sqrt{\frac{2M_e G}{R_e}}$

For planet : $v_p = \sqrt{\frac{2M_p G}{R_p}}$

Therefore, $\frac{v_p}{v_e} = \sqrt{\frac{M_p \cdot R_e}{M_e \cdot R_p}}$ (i)

If ρ_p and ρ_e are the respective average densities of the planet and the earth, then

$$M_p = \frac{4\pi}{3} R_p^3 \rho_p$$

and $M_e = \frac{4\pi}{3} R_e^3 \rho_e$

Therefore, $\frac{M_p}{M_e} = \frac{R_p^3}{R_e^3}$ ($\because \rho_p = \rho_e$) (ii)

Using (ii) in (i) we get

$$\frac{v_p}{v_e} = \frac{R_p}{R_e} = 2 \quad (\because R_p = 2R_e)$$

or $v_p = 2v_e$. Hence the correct choice is (3).

Q10. Choose the wrong statement. The escape velocity of a body from a planet depends upon

- a. the mass of the body
- b. the mass of the planet
- c. the average radius of the planet
- d. the average density of the planet

Sol: a

The escape velocity depends on the mass of the planet, its radius and its density.

Q11. A rocket is fired from the earth to the moon. The distance between the earth and the moon is r and the mass of the earth is 81 times the mass of the moon. The gravitational force on the rocket will be zero, when its distance from the moon is

- a. $\frac{r}{20}$
- b. $\frac{r}{15}$
- c. $\frac{r}{10}$
- d. $\frac{r}{5}$

Sol: c

Let the rocket be at a distance x from the moon when the gravitational force on it is zero. Its distance from earth = $r - x$. Gravitational force on the rocket due to earth is

$$F_e = \frac{GmM_e}{(r-x)^2}$$

where m is the mass of the rocket. Gravitational force on the rocket due to moon is

$$F_m = \frac{GmM_m}{x^2}$$

Since the two forces are in opposite directions, the net force on the rocket will be zero if $F_e = F_m$. Equating the two we get

$$\frac{r-x}{x} = \sqrt{\frac{M_e}{M_m}} = \sqrt{81} = 9$$

which gives $x = \frac{r}{10}$. Hence the correct choice is (3).

Q12. Two spheres, each of mass M , are placed at a distance r apart on a horizontal surface. The gravitational field intensity at the midpoint of the line joining the centres of the spheres is

- a. zero
- b. $\frac{GM^2}{r^2}$
- c. $\frac{GM^2}{2r^2}$
- d. $\frac{GM^2}{4r^2}$

Sol: a

Gravitational field intensity at a point is defined as the gravitational force experienced by a unit mass placed at that point. Since, the spheres have the same mass, the gravitational forces exerted by each sphere on a unit mass placed at the midpoint will be equal and opposite. Hence, the gravitational field intensity at the mid-point is zero. Thus the correct option is 1.

Q13. The escape velocity of a body on the earth's surface is v_e . A body is thrown with a speed $3v_e$. Assuming that the sun and the planets do not influence the motion of the body, its speed at infinity will be

- a. zero
- b. v_e
- c. $\sqrt{2} v_e$
- d. $2\sqrt{2} v_e$

Sol: d

If v_i and v_f are respectively the initial and final speeds of the body, we have, from the law of conservation of energy,

$$\frac{1}{2} m v_i^2 - \frac{GmM}{R} = \frac{1}{2} m v_f^2 \quad \text{(i)}$$

where m is the mass of the body and M is the mass of the earth and R its radius. The escape velocity is given by

$$\frac{1}{2} m v_e^2 = \frac{GmM}{R} \quad \text{(ii)}$$

Using (ii) in (i) gives

$$\frac{1}{2} m v_i^2 - \frac{1}{2} m v_e^2 = \frac{1}{2} m v_f^2$$

or $v_f = (v_i^2 - v_e^2)^{1/2} \quad \text{(iii)}$

Given $v_i = 3v_e$. Therefore, $v_f = 2\sqrt{2} v_e$. Hence the correct choice is (4).

Q14. The radius of the earth is R . For a satellite to appear stationary, it must be placed in orbit around the earth at a height of about (given $R = 6380$ km)

- a. $5.6 R$
- b. $6.6 R$

- c. 7.6 R
- d. 8.6 R

Sol: a

For a geostationary satellite, $h = 35870$ km

$$\therefore \frac{h}{R} = \frac{35870}{6380} = 5.6, \text{ which is choice (1).}$$

Q15. Choose the only incorrect statement from the following

- a. The equivalence of inertial and gravitational mass has provided a clue to the deeper understanding of gravitation.
- b. At poles, the effect of rotation of the earth on the value of g is the minimum.
- c. Massive rockets and extremely tiny particles, such as the molecules of a gas, require the same initial velocity to escape from the earth.
- d. A geostationary satellite, if imparted the necessary velocity, can be put in orbit at any height above the earth.

Sol: d

The only incorrect statement is (4). A geostationary satellite can be put in orbit only at a height of 35,870 km above the earth.

Q16. Infinite number of masses, each of mass m , are placed along a straight line at distances of r , $2r$, $4r$, $8r$, etc. from a reference point O . The gravitational field intensity at point O will be

- a. $\frac{5 Gm}{4r^2}$
- b. $\frac{4 Gm}{3r^2}$

- c. $\frac{3 Gm}{2r^2}$
d. $\frac{2 Gm}{r^2}$

Sol: b

The gravitational field intensity at point O will be

$$\begin{aligned} I &= Gm \left[\frac{1}{r^2} + \frac{1}{(2r)^2} + \frac{1}{(4r)^2} + \frac{1}{(8r)^2} + \dots \right] \\ &= \frac{Gm}{r^2} \left[1 + \frac{1}{2^2} + \frac{1}{4^2} + \frac{1}{8^2} + \dots \right] \\ &= \frac{Gm}{r^2} \left[\frac{1}{2^0} + \frac{1}{2^2} + \frac{1}{2^4} + \frac{1}{2^6} + \dots \right] \\ &= \frac{Gm}{r^2} \left(\frac{1}{1 - \frac{1}{2^2}} \right) = \frac{Gm}{r^2} \left(\frac{1}{1 - \frac{1}{4}} \right) = \frac{4Gm}{3r^2} \end{aligned}$$

Hence the correct choice is (2).

- Q17. A body of mass m is raised to a height h above the surface of the earth of mass M and radius R until its gravitational potential energy increases by $\frac{1}{3} mgR$.
The value of h is

- a. $\frac{R}{3}$
b. $\frac{R}{2}$
c. $\frac{mR}{(M+m)}$
d. $\frac{mR}{M}$

Sol: b

$$\text{PE on the surface of earth} = -\frac{GMm}{R}$$

PE at a height h above the surface of earth

$$= -\frac{GMm}{(R+h)}$$

$$\therefore \text{Increase in PE} = -\frac{GMm}{(R+h)} - \left(-\frac{GMm}{R}\right)$$

$$= GMm \left(\frac{1}{R} - \frac{1}{R+h}\right)$$

$$= GMm \left[\frac{h}{R(R+h)}\right]$$

$$= \frac{gRmh}{(R+h)} \quad \left(\because g = \frac{GM}{R^2}\right)$$

\therefore PE will increase by $\frac{1}{3}mgR$ at a value of h given by

$$\frac{gRmh}{(R+h)} = \frac{1}{3}mgR$$

or $\frac{h}{R+h} = \frac{1}{3}$ or $h = \frac{R}{2}$, which is choice (2).

Q18. The change in the gravitational potential energy when a body of mass m is raised to a height nR above the surface of the earth is (here R is the radius of the earth)

- a. $\left(\frac{n}{n+1}\right)mgR$
- b. $\left(\frac{n}{n-1}\right)mgR$
- c. $nmgR$
- d. $\frac{mgR}{n}$

Sol: a

$$\text{Change in PE} = \frac{GMm}{R} - \frac{GMm}{(n+1)R} = \left(\frac{n}{n+1}\right)mgR$$

Hence the correct choice is (1).

Q19. Two solid spheres of radii r and $2r$, made of the same material are kept in contact. The mutual gravitational force of attraction between them is proportional to

- a. $\frac{1}{r^4}$
- b. $\frac{1}{r^2}$
- c. r^2
- d. r^4

Sol: d

If ρ is the density of the material of each sphere, then the mass of the sphere of radius r is $M_1 = \frac{4\pi}{3}r^3\rho$ and the mass of the sphere of radius $2r$ is

$$M_2 = \frac{4\pi}{3}(2r)^3\rho.$$

Distance between their centres is $d = r + 2r = 3r$.

$$\text{Now } F = \frac{GM_1M_2}{d^2} = \frac{G \times \left(\frac{4\pi}{3}\right)r^3\rho \times \frac{4\pi}{3}(2r)^3\rho}{9r^2}$$

which gives $F \propto r^4$, which is choice (4).

Q20. A comet is moving in a highly elliptical orbit around the sun. When it is closest to the sun, its distance from the sun is r and its speed is v . When it is farthest from the sun, its distance from the sun is R and its speed will be

- a. $v \left(\frac{r}{R} \right)^{1/2}$
- b. $v \left(\frac{r}{R} \right)$
- c. $v \left(\frac{r}{R} \right)^{3/2}$
- d. $v \left(\frac{r}{R} \right)^2$

Sol: b

The angular momentum of the planet is constant over the entire orbit. Hence $vr = VR$ or $V =$

$v \left(\frac{r}{R} \right)$, which is choice (2).