

Class: XII
Subject: Maths
Topic: Differential Equation
No. of Questions: 24

- Q1. Consider the differential equation $\frac{dy}{dx} = \frac{y}{2y \log y + y - x}$
- A. Statement – 1 is true, statement – 2 is true and statement – 2 is the correct explanation for statement – 1.
B. Statement – 1 is true, statement – 2 is true and statement – 2 is not the correct explanation for statement – 1.
C. Statement – 1 is true, statement – 2 is false.
D. Statement – 1 is false, statement – 2 is true.
- Q2. Statement – 1: The differential equation of all circles in a plane must be of order 3.
Statement – 2 : There is only one circle passing through three non-collinear points.
- A. Statement – 1 is true, statement – 2 is true and statement – 2 is the correct explanation for statement – 1.
B. Statement – 1 is true, statement – 2 is true and statement – 2 is not the correct explanation for statement – 1.
C. Statement – 1 is true, statement – 2 is false.
D. Statement – 1 is false, statement – 2 is true.
- Q3. Statement -1: Curve satisfying the differential equation $y' = y/2x$ through (2,1) is a parabola with focus (1/4, 0)
- Statement – 2: The differential equation $y' = y/2x$ is of variable separable form.
- A. Statement – 1 is true, statement – 2 is true and statement – 2 is the correct explanation for statement – 1.
B. Statement – 1 is true, statement – 2 is true and statement – 2 is not the correct explanation for statement – 1.
C. Statement – 1 is true, statement – 2 is false.
D. Statement – 1 is false, statement – 2 is true.

Q4 Let a solution $y = y(x)$ of the differential equation $x\sqrt{x^2 - 1} dy - y\sqrt{y^2 - 1} dx = 0$ satisfy $y(2) = 2\sqrt{3}$

Statement – 1: $y(x) = \sec(\sec^{-1} x - \pi/6)$

Statement – 2: $y(x)$ is given by $\frac{1}{y} = \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}}$

- A. Statement – 1 is true, statement – 2 is true and statement – 2 is the correct explanation for statement – 1.
- B. Statement – 1 is true, statement – 2 is true and statement – 2 is not the correct explanation for statement – 1.
- C. Statement – 1 is true, statement – 2 is false.
- D. Statement – 1 is false, statement – 2 is true.

Q5. Let $(xy^2 + x)dx + (y - x^2y)dy = 0$ satisfy $y(0) = 0$.

Statement – 1: The curve represented by the solution of the given differential equation is a circle.

Statement – 2: It is circle with radius 1 and centre (0, 0).

- A. Statement – 1 is true, statement – 2 is true and statement – 2 is the correct explanation for statement – 1.
- B. Statement – 1 is true, statement – 2 is true and statement – 2 is not the correct explanation for statement – 1.
- C. Statement – 1 is true, statement – 2 is false.
- D. Statement – 1 is false, statement – 2 is true.

Q6. Let $y' + \sin \frac{x+y}{2} = \sin \frac{x-y}{2}$

Statement – 1: A solution satisfying $y(0) = \pi$ is a periodic function with period 4π .

Statement – 2: y can be explicitly represented in terms of x .

- A. Statement – 1 is true, statement – 2 is true and statement – 2 is the correct explanation for statement – 1.
- B. Statement – 1 is true, statement – 2 is true and statement – 2 is not the correct explanation for statement – 1.
- C. Statement – 1 is true, statement – 2 is false.
- D. Statement – 1 is false, statement – 2 is true.

- Q7. Let $f(x)$ be differentiable on the interval $(0, \infty)$ such that $f(1) = 1$, and $\lim_{t \rightarrow x} \frac{t^2 f(x) - x^2 f(t)}{t - x} = 1$ for each $x > 0$. Then $f(x)$ is

- A. $\frac{1}{3x} + \frac{2x^2}{3}$
 B. $-\frac{1}{3x} + \frac{4x^2}{3}$
 C. $-\frac{1}{x} + \frac{2}{x^2}$
 D. $\frac{1}{x}$

- Q8. Let I be the purchase value of an equipment and $V(t)$ be the value after it has been used for t years. The value $V(t)$ depreciates at a rate given by differential equation

$$\frac{dV(t)}{dt} = -k(T - t), \quad \text{where } k > 0 \text{ is a constant and } T \text{ is the total life in years of the equipment.}$$

Then the scrap value $V(T)$ of the equipment is:

- A. e^{-kT}
 B. $T^2 - \frac{1}{k}$
 C. $I - \frac{kT^2}{2}$
 D. $I - k(T)$

- Q9. The solution of $x^3 \frac{dy}{dx} + 4x^2 \tan y = e^x \sec y$ satisfying $y(1) = 0$ is

- A. $\tan y = (x - 2) e^x \log x$
 B. $\sin y = e^x (x - 1) x^{-4}$
 C. $\tan y = (x - 1) e^x x^{-3}$
 D. $\sin y = e^x (x - 1) x^{-3}$

- Q10. A solution of the equation $x \frac{dy}{dx} = y (\log y - \log x + 1)$ is
- A. $y = xe^{cx}$
 - B. $y^2/x = cx$
 - C. $y^2 = cx \log x$
 - D. $\log y = cx$
- Q11. The population $p(t)$ at time t of a certain mouse species follows the differential equation $\frac{dp(t)}{dt} = 0.5 p(t) - 450$. If $p(0) = 850$, then the time at which the population becomes zero is
- A. $\log 9$
 - B. $\frac{1}{2} \log 18$
 - C. $\log 18$
 - D. $2 \log 18$
- Q12. The degree and order respectively of the differential equation of all parabolas whose axis is x -axis, are:
- A. 2, 1
 - B. 1, 2
 - C. 2, 2
 - D. 1, 1
- Q13. The equation of the curve whose tangent at any point (x, y) makes an angle $\tan^{-1}(2x + 3y)$ with x -axis and which passes through $(1, 2)$ is:
- A. $6x + 9y + 2 = 26e^{3(x-1)}$
 - B. $6x - 9y + 2 = 26e^{3(x-1)}$
 - C. $6x + 9y - 2 = 26e^{3(x-1)}$
 - D. $6x - 9y - 2 = 26e^{3(x-1)}$

Q14. If for the differential equation $y' = \frac{y}{x} + \phi\left(\frac{x}{y}\right)$ the general solution is $y = \frac{x}{\log |Cx|}$ then $\phi(x/y)$ is given by

- A. $-x^2/y^2$
- B. y^2/x^2
- C. x^2/y^2
- D. $-y^2/x^2$

Q15. The solution $y(x)$ of the differential equation $\frac{d^2y}{dx^2} = \sin 3x + e^x + x^2$ when $y_1(0) = 1$ and $y(0) = 0$ is

- A. $-\frac{\sin 3x}{9} + e^x + \frac{x^4}{12} + \frac{1}{3}x - 1$
- B. $-\frac{\sin 3x}{9} + e^x + \frac{x^4}{12} + \frac{1}{3}x$
- C. $-\frac{\cos 3x}{3} + e^x + \frac{x^4}{12} + \frac{1}{3}x + 1$
- D. none of these

Q16. The differential equation $\frac{dy}{dx} = \frac{\sqrt{1-y^2}}{y}$ determines a family of circles with

- A. variable radii and a fixed centre (0, 1)
- B. variable radii and a fixed centre (0, -1)
- C. fixed radius 1 and a variable centres along the x-axis
- D. fixed radius 1 and variable centres along the y-axis

Q17. The orthogonal trajectories of the family of curves $a^{n-1}y = x^n$ are given by

- A. $x^n + n^2y = \text{const}$
- B. $ny^2 + x^2 = \text{const}$
- C. $n^2x + y^n = \text{const}$
- D. $n^2x - y^n = \text{const}$

Q18. The solution of the differential equation $\frac{d^2x}{dt^2} + x = 0$; $x(0) = 1, x'(0) = 0$

- A. approaches infinity as $t \rightarrow \infty$
- B. is a periodic function
- C. is always greater than or equal to unity
- D. does not exist

Q19. The solution of differential equation $\frac{dy}{dx} = \frac{y}{x} + 2 \frac{\phi(y/x)}{\phi'(y/x)}$ is

- A. $x^2 \phi(y/x) = k$
- B. $y^2 \phi(y/x) = k$
- C. $\phi(y/x) = k x^2$
- D. $\phi(y/x) = k y^2$

Q20. The degree of the differential equation satisfying $\sqrt{1+x^2} + \sqrt{1+y^2} = A \left(X\sqrt{1+y^2} - y\sqrt{1+x^2} \right)$ is

- A. 2
- B. 3
- C. 4
- D. None of these

Q21. Write the degree of the differential equation

$$\left(\frac{dy}{dx}\right)^4 + 3x \frac{d^2y}{dx^2} = 0.$$

[Delhi 2013]

Q22. Write the differential equation representing the family of curves $y=mx$, where m is an arbitrary constant [All India 2013]

Q23. Find the differential equation of family of circles touching y -axis at the origin.

[Hints; Delhi 2010C; All India 2009C]

- Q24. Form the differential equation representing family of ellipses having foci on X-axis and centre at the origin. [Hots;Delhi 2009C]

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