

Class: XII
Subject: Math's
Topic: Vector Algebra
No. of Questions: 30

Q1. The magnitude of the resultant of vectors $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$ and $\vec{b} = \hat{i} + 2\hat{j} + 3\hat{k}$ is

- A. $\sqrt{6}$
- B. $\sqrt{34}$
- C. $\sqrt{14}$
- D. none of these

Q2. The magnitude of a vector can never be

- A. negative
- B. zero
- C. positive
- D. none of these

Q3. Let \vec{a} be a non-zero vector then $\frac{\vec{a}}{|\vec{a}|}$ is a

- A. null vector
- B. scalar
- C. unit vector parallel to \vec{a}
- D. unit vector perpendicular to \vec{a}

Q4. For any two vectors \vec{a} and \vec{b} which of the following is true?

A. $|\vec{a} + \vec{b}| \geq |\vec{a}| + |\vec{b}|$

B. $|\vec{a} + \vec{b}| = |\vec{a}| + |\vec{b}|$

C. $|\vec{a} + \vec{b}| < |\vec{a}| + |\vec{b}|$

D. $|\vec{a} + \vec{b}| \leq |\vec{a}| + |\vec{b}|$

Q5. A vector with magnitude zero is called a

- A. free vector
- B. localized vector
- C. position vector
- D. null vector

Q6. Which of the following is not a vector quantity?

- A. force
- B. mass
- C. weight
- D. velocity

Q7. If $|\vec{a}| = 3$, $|\vec{b}| = 4$ and $|\vec{a} + \vec{b}| = 5$, then $|\vec{a} - \vec{b}| =$

- A. 6
- B. 5
- C. 4
- D. 3

Q8. If $|\vec{a} + \vec{b}|^2 = |\vec{a}|^2 + |\vec{b}|^2$, then

- A. $|\vec{a} + \vec{b}|^2 = |\vec{a} + \vec{b}|$
- B. $\vec{a} = \vec{b}$
- C. $\vec{a} \perp \vec{b}$
- D. $\vec{a} \parallel \vec{b}$

Q9. If \vec{a} and \vec{b} are non-collinear proper vectors, then number of unit vectors at right angles to both \vec{a} and \vec{b} is

- A. 1
- B. 2
- C. 4
- D. infinitely many

Q10. The vectors $2\hat{i} + 3\hat{j} - 6\hat{k}$ and $a\hat{i} + b\hat{j} + c\hat{k}$ are perpendicular when

- A. $a = 1, b = 2, c = 3$
- B. $a = 3, b = 2, c = 1$
- C. $a = 6, b = 2, c = 3$
- D. None of these

Q11. What is the value of $(a.i)i + (a.j)j + (a.k)k$?

- A. a
- B. $2a$
- C. 0
- D. None of these

Q12. If $|\vec{a} \times \vec{b}| = |\vec{a} \cdot \vec{b}|$, then the angle between \vec{a} and \vec{b} is

- A. $\pi/3$
- B. $\pi/6$
- C. $\pi/2$
- D. $\pi/4$

Q13. If the vectors $2\hat{i} + 3\hat{j} - 4\hat{k}$ and $a\hat{i} + b\hat{j} + c\hat{k}$ are at right angles, then a, b, c can have values

- A. $a = 2, b = 3, c = -4$
- B. $a = 4, b = 4, c = 5$
- C. $a = 4, b = 4, c = -5$
- D. $a = 4, b = -4, c = -5$

Q14. $[\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}] =$

- A. $[\vec{a} \vec{b} \vec{c}]$
- B. $2[\vec{a} \vec{b} \vec{c}]$
- C. $[\vec{a} \vec{b} \vec{c}]^2$
- D. none of these

Q15. The distance of the point (x, y, z) from the XY-plane is

- A. x
- B. y
- C. z
- D. $|z|$

Q16. If I is the incentre of triangle ABC, then $|BC| \vec{IA} + |CA| \vec{IB} + |AB| \vec{IC}$ is equal to (Here \vec{A} means magnitude.)

- A. $\frac{|\vec{A} + \vec{B} + \vec{C}|}{3}$
- B. $|\vec{A} + \vec{B} + \vec{C}|$
- C. $\vec{0}$
- D. None of these

Q17. If ABCDEF is a regular hexagon and

$\vec{AB} = \vec{a}, \vec{BC} = \vec{b}$, \vec{AD} is equal to

- A. $\vec{a} + \vec{b}$
- B. $\vec{b} - \vec{a}$
- C. $2\vec{b}$
- D. None of these

Q18. If $\vec{a} \cdot \vec{a} = 0$, then \vec{a} is a

- A. free vector
- B. localized vector
- C. null vector
- D. none of these

Q19. In a triangle ABC, D is the mid-point of side [BC]; \vec{AD} is equal to

- A. $\vec{AB} + \vec{AC}$
- B. $\frac{1}{2}(\vec{AB} + \vec{AC})$
- C. $\vec{AB} - \vec{AC}$
- D. None of these

Q20. The medians of a triangle are concurrent at the point called

- A. Circumcentre
- B. Orthocentre
- C. Centroid
- D. Incentre

Q21. P and Q are two points with position vectors $3\vec{a} - 2\vec{b}$ and $\vec{a} + \vec{b}$, respectively. Write the position vector of a point R divides the line segment PQ in the ratio 2 : 1 externally.

[All India 2013]

- Q22. Write the position vector of mid-point of the vector joining points P (2, 3, 4) and Q (4, 1 - 2).
[Foreign 2011]
- Q23. Find the position vector of a point R, which divides the line joining two points P and Q whose position vectors are $2\vec{a} + \vec{b}$ and $\vec{a} - 3\vec{b}$ respectively, externally in the ratio 1 : 2. Also, show that P is the mid-point of line segment RQ.
[Hots; Delhi 2010]
- Q24. Find $|\vec{x}|$, if for a unit vector \hat{a} , $(\vec{x} - \hat{a}) \cdot (\vec{x} + \hat{a}) = 15$.
[Hots; All India 2013]
- Q25. Write the value of $(\hat{k} \times \hat{j}) \cdot \hat{i} + \hat{j} \cdot \hat{k}$.
[Hots; All India 2012]
- Q26. If \hat{P} is a unit vector and $(\vec{X} - \hat{P}) \cdot \vec{X} + \hat{P} = 80$, then find $|\vec{X}|$.
[Hots; All India 2009]
- Q27. If $\vec{a} + \vec{b} + \vec{c}$ are three vectors, such that $|\vec{a}| = 5$, $|\vec{b}| = 12$, $|\vec{c}| = 13$ and $\vec{a} + \vec{b} + \vec{c} = 0$, then, find the value of $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$.
[Delhi 2012]
- Q28. If vectors $\vec{a} = 2\hat{i} + 2\hat{j} + 3\hat{k}$, $\vec{b} = -\hat{i} + 2\hat{j} + \hat{k}$ and $\vec{c} = 3\hat{i} + \hat{j}$ are such that $\vec{a} + \lambda\vec{b}$ is perpendicular to \vec{c} , then find the value of λ .
- Q29. If \vec{a} , \vec{b} and \vec{c} are three vectors, such that $|\vec{a}| = 3$, $|\vec{b}| = 4$ and $|\vec{c}| = 5$ and each one of these is perpendicular to the sum of other two, then find $|\vec{a} + \vec{b} + \vec{c}|$.
[All India 2011C, 2010C]
- Q30. If \vec{a} , \vec{b} , \vec{c} are such that $\vec{a} + \vec{b} + \vec{c} = 0$ and $|\vec{a}| = 3$, $|\vec{b}| = 5$ and $|\vec{c}| = 7$, then find angle between \vec{a} and \vec{b} .
[All India 2008; Delhi 2008]

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