

Class: 9
Subject: Mathematics
Topic: Lines and Angles
No. of Questions: 20

Q1. If the ratio of three angles of a triangle is 1 : 2 : 3, find the angles.

Sol. Ratio of the three angles of a triangle = 1 : 2 : 3

Let the angles be x , $2x$, and $3x$

$$X + 2X + 3X = 180^\circ$$

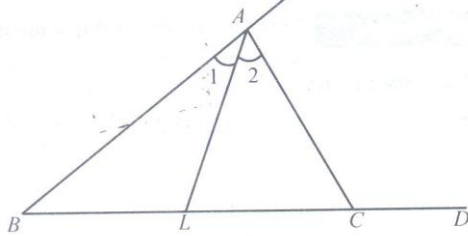
$$\therefore 6X = 180^\circ$$

Hence the first angle = $x = 30^\circ$

The second angle = $2x = 60^\circ$

The third angle = $3x = 90^\circ$

Q2. The side BC of a triangle ABC is produced to D. The bisector of the $\angle A$ meets BC in L. Prove that $\angle ABC + \angle ACD = 2 \angle ALC$



Sol. $\angle ALC = \angle 1 + \angle B$

$$\Rightarrow 2\angle ALC = 2\angle 1 + 2\angle B$$

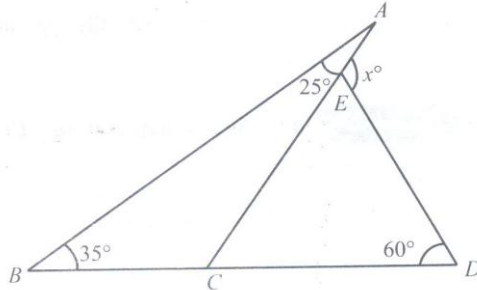
$$\Rightarrow 2\angle ALC = \angle A + 2\angle B$$

$$\Rightarrow 2\angle ALC = (\angle ACD - \angle B) + 2\angle B$$

$$(\because \angle ACD = \angle A + \angle B)$$

$$\Rightarrow 2\angle ALC = \angle ACD + \angle B = \angle ACD + \angle ABC$$

Q3. In the figure, find the value of x°



Sol. In the ΔABC , $\angle A + \angle B + \angle ACB = 180^\circ$

$$\Rightarrow 25^\circ + 35^\circ + \angle ACB = 180^\circ$$

$$\Rightarrow \angle ACB = 120^\circ$$

$$\text{Now } \angle ACB + \angle ACD = 180^\circ \quad [\text{linear pair}]$$

$$\text{Or } 120^\circ + \angle ACD = 180^\circ$$

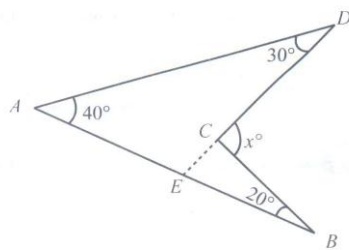
$$\text{Or } \angle ACD = 60^\circ = \angle EDC$$

Again in the ΔCDE , CE is produced to A.

$$\text{Hence, } \angle AED = \angle ECD + \angle EDC$$

$$\Rightarrow x = 60^\circ + 60^\circ = 120^\circ$$

Q4. In the given figure find the value of x°



Sol. Produced DC such that it meets AB in E

Now in the ΔAED ,

Side AE is produced to B

$$\therefore \angle DEB = \angle EDA + \angle DAE \quad [\text{Ext. angle of a triangle}]$$

$$\angle DEB = 30^\circ + 40^\circ = 70^\circ = \angle CEB$$

Now in the ΔBEC ,

Side EC is produced to D

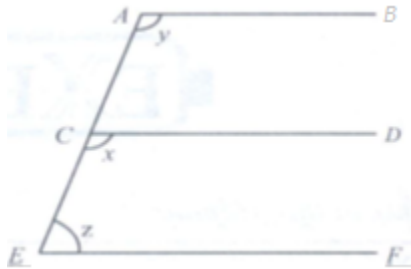
$$\therefore \angle DCB = \angle CEB + \angle CBE \quad [\text{Ext. angle of a triangle}]$$

$$\begin{aligned}\therefore \angle DCB &= 70^\circ + 20^\circ = 90^\circ \\ \Rightarrow x^\circ &= 90^\circ\end{aligned}$$

Q5. An angle is 16° more than its complement. What is its measure?

Sol. Let one angle = a°
Then second angle = $(a+16)^\circ$
Now, $a+(a+16) = 90^\circ$
 $\Rightarrow 2a+16 = 90^\circ \Rightarrow a = 37^\circ$
Second angle = $37^\circ + 16^\circ = 53^\circ$

Q6. In the given figure, AB, CD and EF are parallel. If $\angle z = 70^\circ$, find the value of x and y.

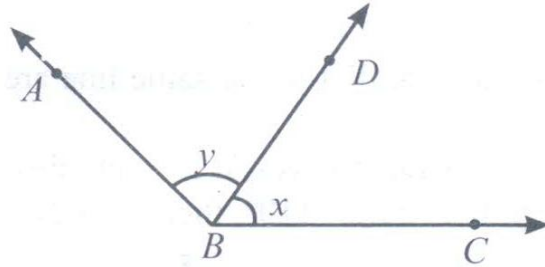


Sol. $x = y = 110^\circ$

Q7. Why is Axiom 5, in the list of Euclid's axiom, considered a 'universal truth'? (Note the question is not about the fifth postulate).

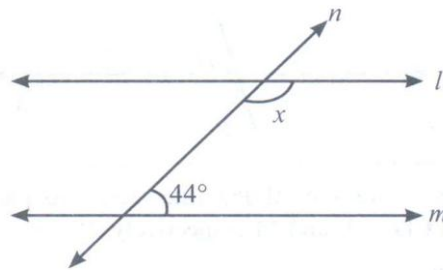
Sol. This is true for anything in any part of the world, this is a universal truth.

Q8. For what value of $x+y$ in the given figure, will ABC be a line? Justify your answer.



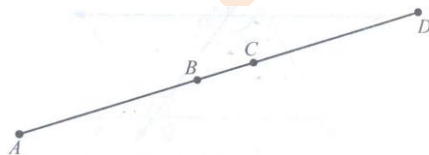
Sol. For A, B, C must be lie in a line $x+y=180^\circ$

Q9. In the given figure, find the value of x for which the lines l and m are parallel.



Sol. $x+44^\circ = 180^\circ$ i.e., $x = 136^\circ$

Q10. If $AC = BD$, then Prove that $AB = CD$



Sol. $AC = BD$... (i)
 $AC = AB + BC$ [B lies between A and C] ... (ii)
 $BD = BC + CD$ [C lies between B and D] ... (iii)
 Substituting (ii) and (iii) in (i), we get
 $AB + BC = BC + CD$
 $\Rightarrow AB = CD$ [Subtracting equals from equal]

Q11. The supplement of an angle is one-fifth of itself. Determine the angle and its supplement.

Sol. Let the measures of the angle be x° , then the measure of its supplementary angles is $180^\circ - x^\circ$.

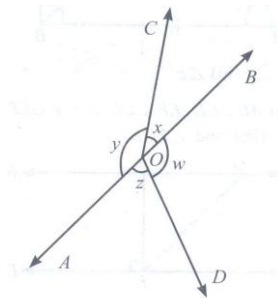
$$\text{It is given that } 180 - x = \frac{1}{5}x$$

$$\Rightarrow 5(180^\circ - x) = x$$

$$\Rightarrow 900 - 5x = x \Rightarrow 900 = 5x + x$$

$$\Rightarrow 900 = 6x \Rightarrow 6x = 900 \Rightarrow x = \frac{900}{6} = 150$$

Q12. In figure, if $x+y = w+z$, then prove that AOB is a line.



Sol. $x+y = w+z$... (i) [Given]

\therefore The sum of all the angles round a point is equal to 360°

$$\therefore x+y+w+z = 360^\circ$$

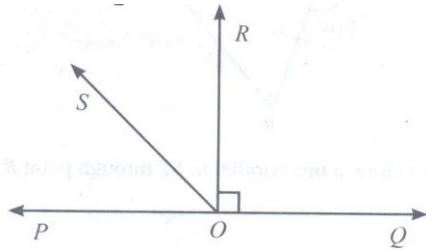
$$\Rightarrow 2(x+y) = 360^\circ$$

$$\Rightarrow x+y = \frac{360^\circ}{2}$$

$$\Rightarrow x+y = 180^\circ$$

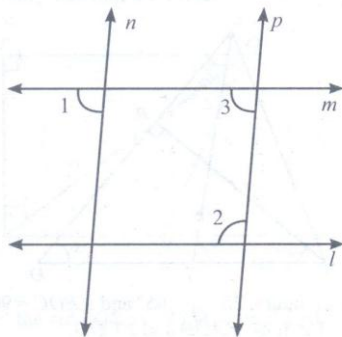
\therefore AOB is a line. (if the sum of two adjacent angles is 180° , then the non-common arms of the angles form a line)

- Q13. In figure, POQ, is a line. Ray OR is perpendicular to line PQ. OS is another ray lying between rays OP and OR. Prove that $\angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$



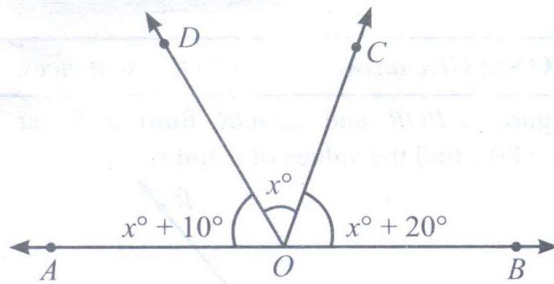
Sol. Since $OR \perp PQ$
 $\therefore \angle QOR = \angle POR = 90^\circ$... (i)
 And $\angle QOS = \angle QOR + \angle ROS$... (ii)
 Also, $\angle POS = \angle POR - \angle ROS$... (iii)
 Subtracting (ii) and (iii),
 $\Rightarrow \angle QOS - \angle POS = (\angle QOS - \angle POR) + 2 \angle ROS$
 $= 2 \angle ROS$ (using (i))
 $\Rightarrow \angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$

- Q14. In figure if $l \parallel m$, $n \parallel p$, and $\angle 1 = 85^\circ$ then find $\angle 2$.



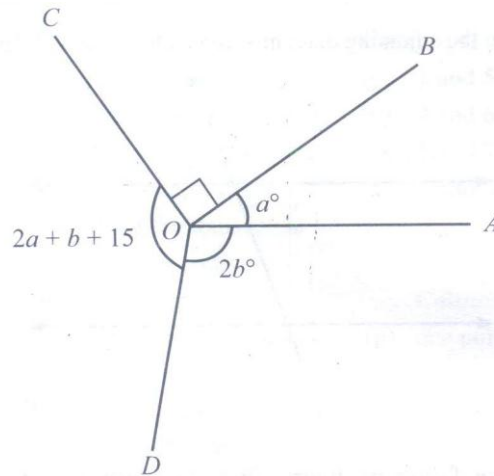
Sol. $\because n \parallel p$ and m is transversal
 $\therefore \angle 1 = \angle 3 = 85^\circ$ (corresponding angles)
 Also, $m \parallel l$ & p is transversal
 $\therefore \angle 2 + \angle 3 = 180^\circ$
 $\Rightarrow \angle 2 + 85^\circ = 180^\circ$
 $\Rightarrow \angle 2 = 180^\circ - 85^\circ$
 $\Rightarrow \angle 2 = 95$

Q15. In the following figure, find $\angle x$. further find $\angle BOC$, $\angle COD$ and $\angle AOD$.



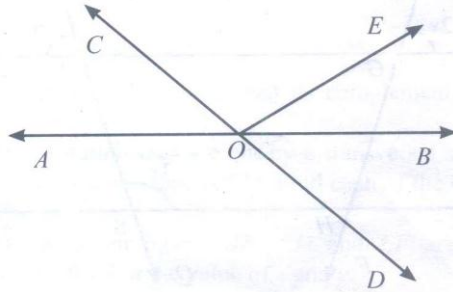
Sol. $X = 50^\circ$, $\angle BOC = 70^\circ$, $\angle COD = 50^\circ$, $\angle AOD = 60^\circ$

Q16. In the given figure $2b - a = 65^\circ$ and $\angle BOC = 90^\circ$, find the measure of $\angle AOB$, $\angle AOD$ and $\angle COD$.



Sol. 35° , 100° , 135°

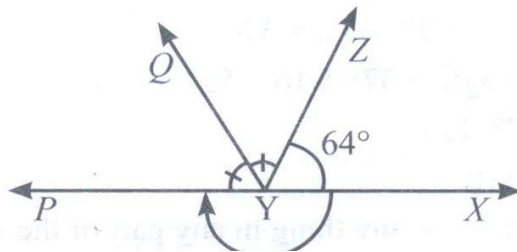
Q17. In figure, Lines AB and CD intersect at O. If $\angle AOC + \angle BOE = 70^\circ$ and $\angle BOD = 40^\circ$, find $\angle BOE$ and reflex $\angle COE$.



Sol. $\angle AOC = \angle BOD$ [Vertically Opposite Angles]
 But Given $\angle BOD = 40^\circ$... (i)
 $\therefore \angle AOC = 40^\circ$ [Alternate Angle] ... (ii)
 Now, Given $\angle AOC + \angle BOE = 70^\circ$
 $\Rightarrow \angle BOE = 70^\circ - 40^\circ$ [From (ii)]
 $\Rightarrow \angle BOE = 30^\circ$
 Again, Reflex $\angle COE = \angle COD + \angle BOD + \angle BOE$
 \because Ray OA stands on line CD
 $= \angle COD + 40^\circ + 30^\circ$ [Using (i) and (ii)]
 $= 180^\circ + 40^\circ + 30^\circ$
 $= 250^\circ$ [\because Ray OA stands on line CD]

Q18. It is given that $\angle XYZ = 64^\circ$ and XY is produced to point P. Draw a figure from the given information. If ray YQ bisects $\angle ZYP$, find $\angle XYQ$ and reflex $\angle QYP$.

Sol. $\angle XYZ + \angle ZYP = 180^\circ$ [Linear pair Axiom and YZ stands on line PX]



Given, $\angle XYZ = 64^\circ$
 $\therefore 64^\circ + \angle ZYP = 180^\circ$
 $\Rightarrow \angle ZYP = 116^\circ$... (i)
 Also, Ray YQ bisect $\angle ZYP$

$$\therefore \angle PYQ = \angle ZYQ = \frac{1}{2} \angle ZYP$$

$$= \frac{1}{2} (116^\circ) = 58^\circ \text{ (Using (i))} \quad \dots(\text{ii})$$

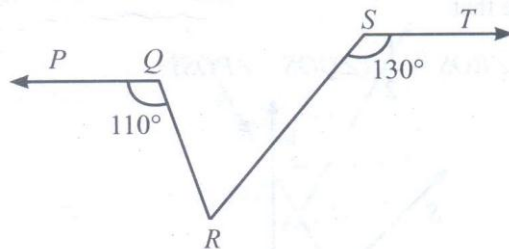
$$\therefore \text{Reflex } \angle QYP = 360^\circ - 58^\circ = 302^\circ \quad [\because \text{The sum of all angles round a point is equal to } 360^\circ]$$

$$\text{Again, } \angle XYQ = \angle XYZ + \angle ZYQ$$

$$= 64^\circ + 58^\circ$$

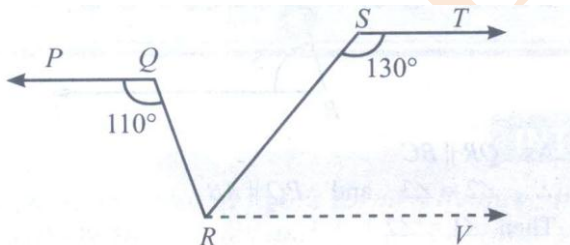
$$= 122^\circ \quad [\because \angle XYZ = 64^\circ \text{ (given) and } \angle ZYQ = 58^\circ \text{ (from (ii))}]$$

Q19. If figure, if $PQ \parallel ST$, $\angle PQR = 110^\circ$ and $\angle RST = 130^\circ$, find $\angle QRS$.



[Hint : Draw a line parallel to ST through point R.]

Sol. Draw a line RV parallel to ST through point R.



$$\therefore \angle RST + \angle SRV = 180^\circ \quad [\because \text{sum of the consecutive interior angles on the same side of the transversal is } 180^\circ]$$

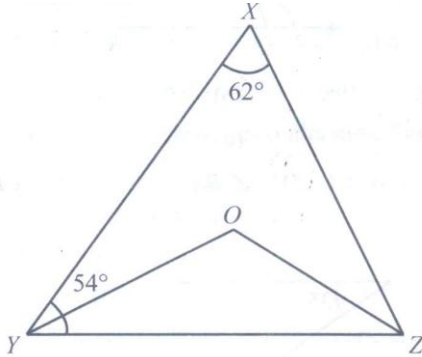
$$\Rightarrow \angle SRV = 180^\circ - 130^\circ = 50^\circ \quad \dots(\text{i})$$

$$\text{Also, } \angle QRV = \angle PQR = 110^\circ \quad [\text{Alternative interior Angles}]$$

$$\Rightarrow \angle QRS + \angle SRV = 110^\circ$$

$$\Rightarrow \angle QRS = 110^\circ - 50^\circ = 60^\circ \quad [\text{Using (i)}]$$

Q20. In figure, $\angle X = 62^\circ$, $\angle XYZ = 54^\circ$. If YO and ZO are the bisectors of $\angle XYZ$ and $\angle YZX$, find $\angle OZY$ and $\angle YOZ$



Sol. From $\triangle XYZ$, we have

$$\begin{aligned}\angle XYZ + \angle YZX + \angle ZXY &= 180^\circ && \text{[By } \Delta\text{'s angle sum property]} \\ \Rightarrow 54^\circ + \angle YZX + 62^\circ &= 180^\circ \\ \Rightarrow \angle YZX &= 180^\circ - 116^\circ = 64^\circ && \dots(i)\end{aligned}$$

Given YO is the bisector of $\angle XYZ$

$$\therefore \angle XYO = \angle OYZ = \frac{1}{2} \angle XYZ = \frac{1}{2} (54^\circ) = 27^\circ \quad \dots(ii)$$

Similarly

$$\angle XZO = \angle OZY = \frac{1}{2} \angle YZX = \frac{1}{2} (64^\circ) = 32^\circ \quad \dots(iii)$$

(\because ZO is the bisector $\angle YZX$)

Now. Consider $\triangle OYZ$, which gives

$$\begin{aligned}\angle OYZ + \angle OZY + \angle YOZ &= 180^\circ && \text{[BY angle sum property]} \\ \Rightarrow 27^\circ + 32^\circ + \angle YOZ &= 180^\circ && \text{[Using (ii) and (iii)]} \\ \Rightarrow \angle YOZ &= 180^\circ - 59^\circ = 121^\circ.\end{aligned}$$

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