

Class: 9
Subject: Physics
Topic: Basic Mathematics Application
No. of Questions: 20

1. What is the difference between A° and A.U.?

Solution:

A° and A. U. both are the units of distances but $1A^\circ = 10^{-10}$ and $1A.U. = 1.496 \times 10^{11}m$.

2. Define S.I. unit of solid angle?

Solution:

One Steradian is defined as the angle made by a spherical plane of area 1 square meter at the center of a sphere of radius 1 m.

3. Name physical quantities whose units are electron volt and Pascal?

Solution:

Energy and Pressure.

4. When a planet X is at a distance of 824.7 million kilometers from earth its angular diameter is measured to be 35.7211° of arc. Calculate the diameter of 'X'.

Solution:

$$R = 824.7 \times 10^6$$

$$\theta = 35.72 \text{ of arc in } 3600 \text{ sec(1 hr)}$$

$$\theta = 35.72 \times \frac{\pi}{180} \text{ radian}$$

Diameter $l = ?$

$$l = r\theta$$

$$l = 824.7 \times 10^6 \times 35.72 \times \frac{\pi}{180}$$

$$l = 513.6 \times 10^6 \text{ km}$$

5. A radar signal is beamed towards a planet from the earth and its echo is received seven minutes later. Calculate the velocity of the signal, if the distance between the planet and the earth is $6.3 \times 10^{10} \text{m}$?

Solution:

$$x = c.t/2$$

$$\Rightarrow c = \frac{2x}{t} = \frac{2 \times 6.3 \times 10^{10}}{7 \times 60} = 3 \times 10^8 \text{m/s}$$

6. Give two methods for measuring time intervals?

Solution:

(A) Radioactive dating – to know age of fossil fuels rocks etc.

(B) Atomic clocks – used to note periodic vibrations taking place within two atoms.

7. Find the dimensions of latent heat and specific heat?

Solution:

(A) Latent Heat = $\frac{Q(\text{Heat Energy})}{m(\text{mass})}$

$$\text{Latent Heat} = \frac{ML^2T^{-2}}{M} = [M^0L^2T^{-2}]$$

(B) Specific heat = (s) = $\frac{Q}{m \times T} = \frac{ML^2T^{-2}}{M \times K}$

$$(s) = [M^0L^2T^{-2}K^{-1}]$$

8. In Vander Waal's equation $\left(P + \frac{a}{V^2}\right) (V - b) = RT$

Solution: $P = a/V^2 \Rightarrow a = PV^2$

$$A = \frac{F}{A} \times V^2$$

$$A = \frac{MLT^{-2}}{L^2} \times [L^3]^2$$

$$A = \frac{MLT^{-2}L^6}{L^2}$$

$$A = [ML^5T^{-2}]$$

Also $b = V$

$$V = [M^0L^3T^0]$$

9. E, M, I and G denote energy, mass, angular momentum and gravitational constant respectively.

Determine the dimensions of EL^2/m^5G^2

- (A) $E = [ML^2T^{-2}]$
 (B) $L = [ML^2T^{-1}]$
 (C) $m = [M]$
 (D) $G = [M^{-1}L^3T^{-2}]$

Solution:

$$\begin{aligned} \therefore \text{Dimensions of } EL^2/m^5G^2 &= \frac{[ML^2T^{-2}][ML^2T^{-1}]^2}{[M]^5[M^{-1}L^3T^{-2}]^2} \\ &= \frac{M^3L^6T^{-4}}{M^3L^6T^{-4}} = 1 \end{aligned}$$

Thus, it is dimensionless

10. (A) State which of the following are dimensionally correct

- (i) Pressure = Energy per unit volume
 (ii) Pressure = Momentum \times volume \times time

(B) The density of cylindrical rod was measured by the formula: - $P = \frac{4m}{\pi D^2L}$. The percentage in m, D and L are 1%, 1.5% and 0.5%. Calculate the % error in the calculated value of density?

Solution:

(A) (i) Pressure = $F/A = \frac{MLT^{-2}}{L^2} = [ML^{-1}T^{-2}]$

$$[ML^{-1}T^{-2}] = \frac{ML^2T^{-2}}{L^3}$$

$$[ML^{-1}T^{-2}] = [ML^{-1}T^{-2}]$$

Hence it is dimensionally correct

(B) $\rho = \frac{4m}{\pi D^2L}$

$$\frac{\Delta\rho}{\rho} = \frac{\Delta m}{m} + 2\frac{\Delta D}{D} + \frac{\Delta L}{L}$$

$$\frac{\Delta\rho}{\rho} \% = 1\% + 2\% \times (1.5)\% + 0.5\%$$

$$\% \frac{\Delta L}{L} = 4.5 \% \Rightarrow \frac{\Delta \rho}{\rho} \% = 4.5 \%$$

11. If $x = at + bt^2$ where x is in meters and t is in seconds. What are the units of a and b ?

Solution:

$$a = \frac{x}{t} = m/s$$
$$b = \frac{x}{t^2} = m/s^2$$

12. Fill ups.

(A) $3.0 \text{ m/s}^2 = \dots\dots\dots \text{ Km / hr}^2$

(B) $6.67 \times 10^{-11} \text{ Nm}^2 / \text{Kg}^2 = \dots\dots\dots \text{ g}^{-1} \text{ cm}^3 \text{ s}^{-2}$

Solution:

(A) $3.0 \text{ m / s}^2 = \frac{3 \times 10^{-3} \text{ km}}{\left(\frac{1}{3600}\right)^2 \text{ hr}^2} = 1080 \text{ km/hr}^2$

(B) $6.67 \times 10^{-11} \text{ Nm}^2 / \text{kg}^2 = \text{g}^{-1} \text{ cm}^3 \text{ s}^{-2} = 6.67 \times 10^{-11} \text{ kg}^{-1} \text{ m}^3 \text{ s}^{-2}$
 $= 6.67 \times 10^{-11} \times 10^{-3} \times (10^2 \text{ cm})^3$
 $= 6.67 \times 10^{-8} \text{ g}^{-1} \text{ cm}^3 \text{ s}^{-2}$

13. Write S.I unit of luminous intensity and temperature?

Solution:

S.I unit of luminous intensity is candela (cd) and of temperature is Kelvin (k).

Calculate the time taken by the light to pass through a nucleus of diameter $1.56 \times 10^{-16} \text{ m}$. (speed of light is $3 \times 10^8 \text{ m/s}$)

14. Time = $\frac{\text{distance}}{\text{velocity}}$

Solution:

$$\text{Time} = \frac{1.56 \times 10^{-16}}{3 \times 10^8}$$

$$T = 5.2 \times 10^{-25} \text{ sec}$$

15. If force (F) acceleration (A) and time (T) are taken as fundamental units, then find the dimension of energy.

Solution:

$$F = MLT^{-2} ; A = LT^{-2} \text{ --- (1)}$$

$$F = MA \Rightarrow M = FA^{-1} \text{--- (2)}$$

$$\text{From equation 1) } L = AT^2$$

$$\therefore \text{Dimensions of energy} = ML^2T^{-2}$$

$$[FA^{-1}A^2T^4T^{-2}] = [FAT^2]$$

16. Two resistances $R_1 = 100 \pm 3 \Omega$ and $R_2 = 200 \pm 4 \Omega$ are connected in series. Then what is the equivalent resistance?

Solution:

$$\text{Here } R_1 = 100 \pm 3 \Omega$$

$$R_2 = 200 \pm 4 \Omega$$

$$\text{In series } R_{\text{net}} = R_1 + R_2$$

$$R_{\text{net}} = (100 \pm 3 \Omega)$$

$$R_{\text{net}} = (200 \pm 4 \Omega)$$

$$R_{\text{net}} = (300 \pm 7) \text{ ohms.}$$

17. If velocity, time and force were chosen the basic quantities, find the dimensions of mass?

Solution:

$$\text{Force} = \text{mass} \times \text{acceleration}$$

$$\text{Force} = \text{mass} \times \frac{\text{velocity}}{\text{time}}$$

$$\frac{\text{time} \times \text{force}}{\text{velocity}} = \text{mass}$$

$$\text{Mass} = \frac{FT}{V}$$

$$\text{Mass} = [FTV^{-1}]$$

18. Young's modulus of steel is $19 \times 10^{10} \text{ N/m}^2$. Express it in dynes cm^2 . Here dynes are the C.G.S. unit of force.

Solution:

$$Y = \frac{[F]}{[L^2]} = \frac{MLT^{-2}}{[L^2]} = [ML^{-1}T^{-2}]$$

Comparing with $M^a L^b T^c$

$$a = 1, b = -1, c = -2$$

$$n_2 = n_1 \left[\frac{M_1}{M_2} \right]^a \left[\frac{L_1}{L_2} \right]^b \left[\frac{T_1}{T_2} \right]^c$$

$$n_2 = 19 \times 10^{10} \left[\frac{1kg}{1g} \right]^1 \left[\frac{1m}{1cm} \right]^{-1} \left[\frac{1S}{1S} \right]^{-2}$$

$$n_2 = 19 \times 10^{10} \left[\frac{1000g}{1g} \right] \left[\frac{100cm}{1cm} \right]^{-1} [1]^{-2}$$

$$n_2 = 19 \times 10^{10} \left[1000 \times \frac{1}{100} \times 1 \right]$$

$$n_2 = 19 \times 10^{11}$$

19. The velocity v of water waves may depend on their wavelength λ density of water ρ and the acceleration due to gravity g . Find relation between these quantities by the method of dimension?

Solution:

$$v \propto \lambda^a \rho^b g^c$$

$$v = K \lambda^a \rho^b g^c \text{ -----(1)}$$

Where K is dimensionless constant

$$[LT^{-1}] = [L]^a [ML^{-3}]^b [LT^{-2}]^c$$

$$[M^0 L T^{-1}] = [L]^{a-3b+c} [M]^b [T]^{-2c}$$

$$a - 3b + c = 1$$

$$b = 0 \Rightarrow a = \frac{1}{2}$$

$$-2c = -1$$

$$c = \frac{1}{2} \text{ Put these values in equation (1)}$$

$$v = k\lambda^{\frac{1}{2}} P^0 g^{\frac{1}{2}}$$

$$v = k\lambda^{\frac{1}{2}} g^{\frac{1}{2}}$$

$$v = k\sqrt{\lambda g}$$

20. The force acting on an object of mass m traveling at velocity v in a circle of radius r is given by $F = \frac{mv^2}{r}$. The measurements recorded as $m = 3.5 \text{ kg} \pm 0.5 \text{m}$. Find the maximum possible (1) fractional error (2) % error in the measurement of force. How will you recorded reading?

Solution:

$$(i) F = \frac{mv^2}{r}$$

$$\frac{\Delta F}{F} = \frac{\Delta m}{m} + 2\frac{\Delta v}{v} + \frac{\Delta r}{r}$$

$$\frac{\Delta F}{F} = \frac{0.1}{3.5} + 2 \times \frac{1}{20} + \frac{0.5}{12.5}$$

$$\frac{\Delta F}{F} = 0.17$$

$$(ii) \% \text{ error in } F = 0.17 \times 100 = 17\%$$

$$(iii) F = \frac{mv^2}{r} = \frac{(3.5) \times (20)^2}{12.5}$$

$$F = 112 \text{ N}$$

$$\Delta F = 19 \text{ N}$$

$$\Delta F = 0.17 \times 112$$

Measurement of force = $F = (112 \pm 19) \text{ N}$